

HD49933:

$$T = \frac{10 - 14.3X}{M^3} \cdot 10^9 \text{ yr}$$

$$V \sin(i) = 10.9 \text{ km/s}$$

$$R \approx 1.5 R_{\text{Sun}} \rightarrow P_{\text{rot}} \approx 7.0 \text{ d}$$

$$\Delta \nu_0 \approx 88.7 \mu\text{Hz}$$

$$\varepsilon \approx 1$$

$$\Delta \nu_0 \approx 135 \mu\text{Hz} \sqrt{M/R^3}$$

$$\nu_{n,l} = \Delta \nu(n + \frac{1}{2}l + \varepsilon) - l(l+1)D_0$$

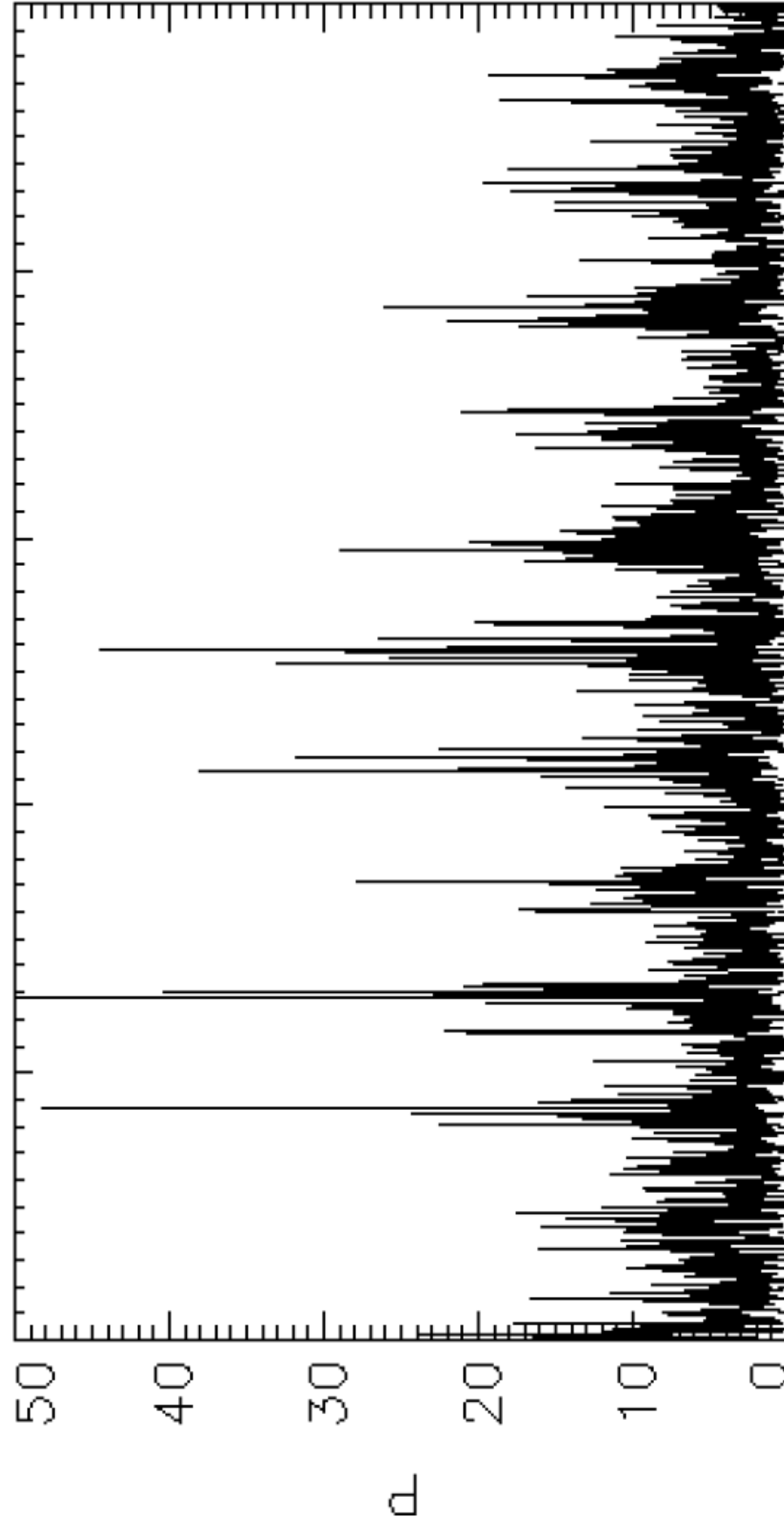
Identify the dominant modes in the spectrum

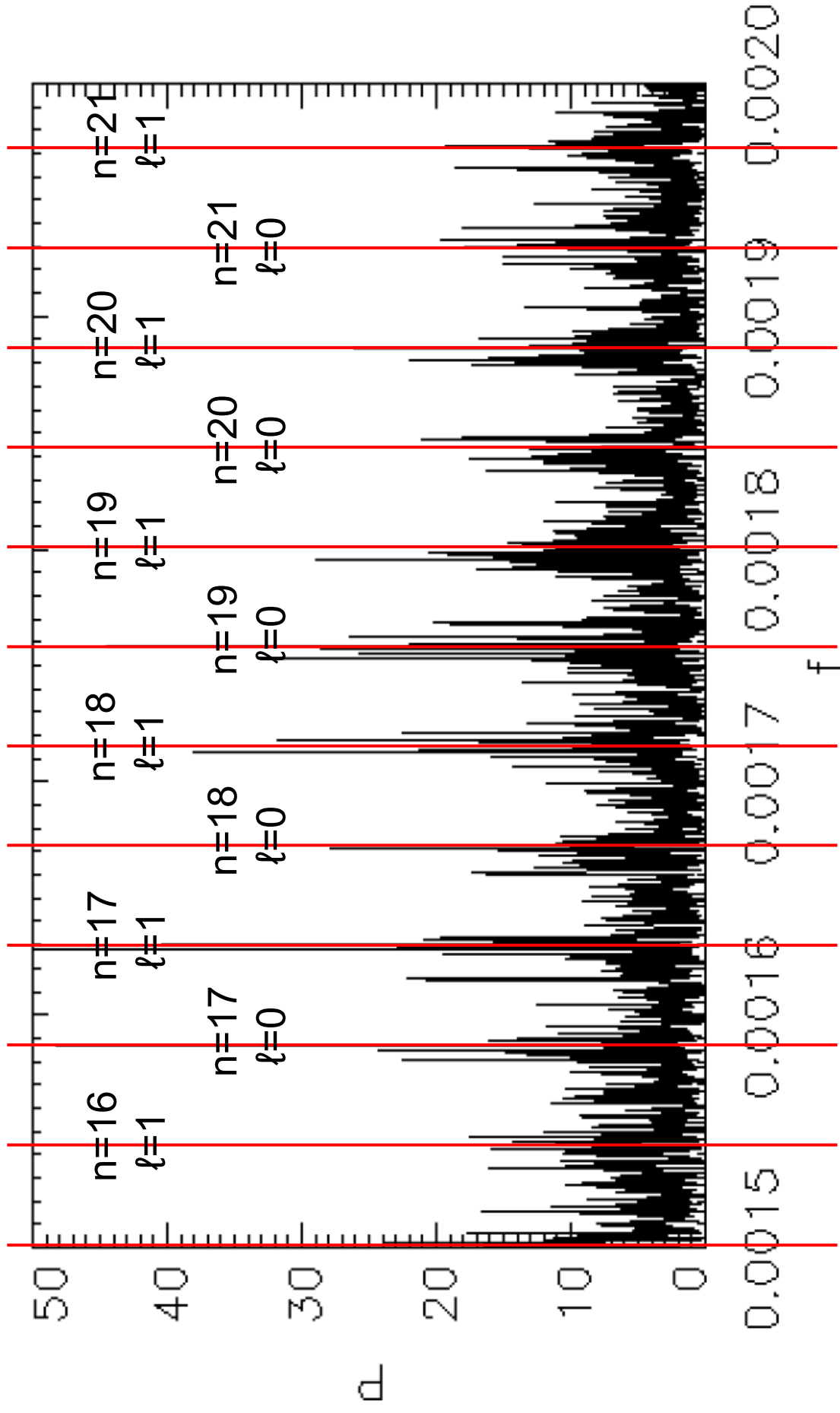
What is its Mass, age and Radius?

What is its rotation period and inclination?

$dI/l \sim 0.001 - 0.003$ for Sunspots

Are the spots on HD49933 of similar size?

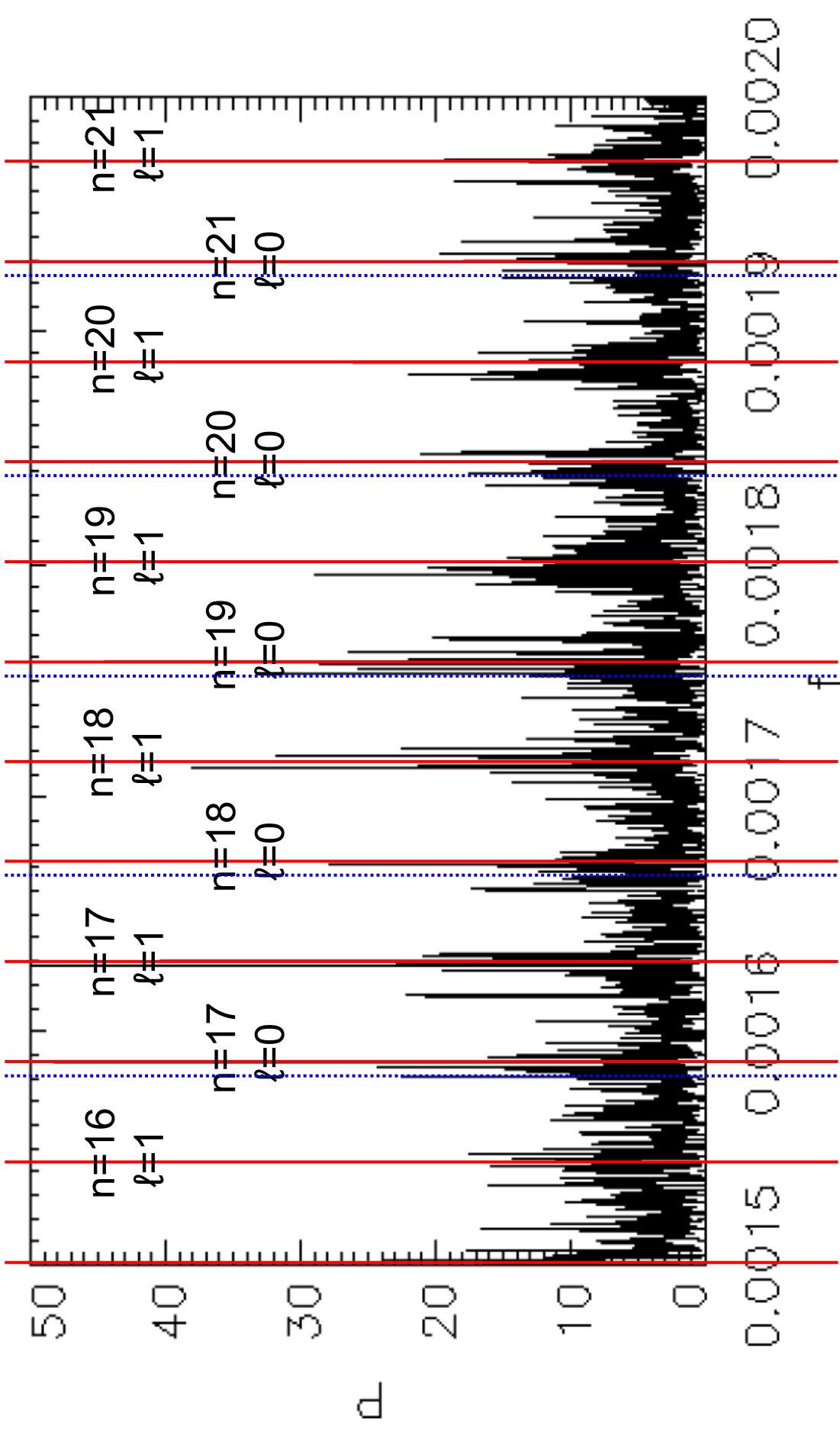




$\Delta\nu_0 = 85.6 \mu\text{Hz}$

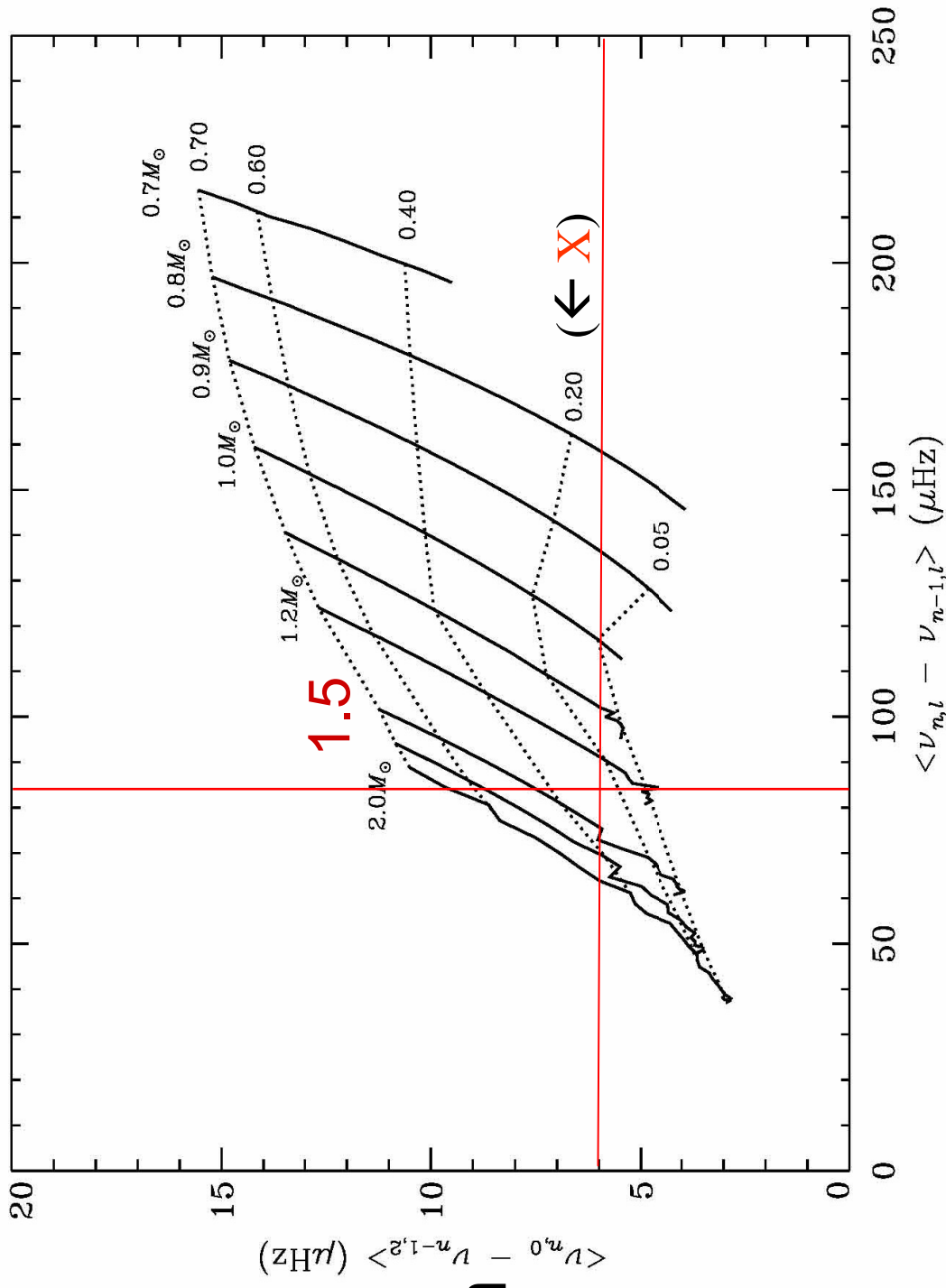
CoRoT: HD 49933

$\Delta\nu_0 = 85.6 \mu\text{Hz}$



Small separation $\sim 6 \mu\text{Hz}$

Theoretical Separations from stellar models:



Small
Separation
(δ_{02})

M ~ 1.3
X ~ 0.23

Large Frequency Separation

HD49933:

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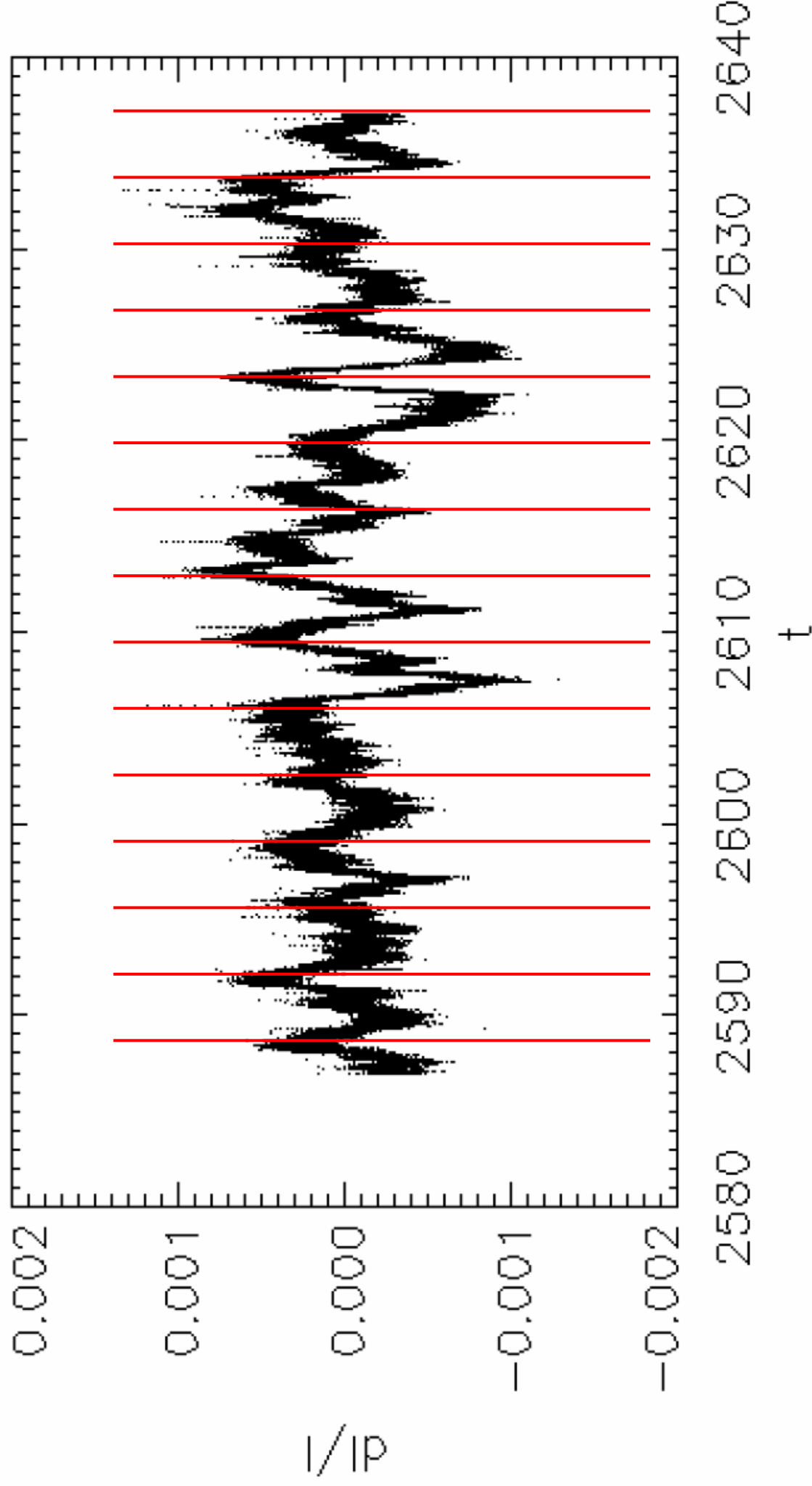
Identify the dominant modes in the spectrum

What is its Mass, age and Radius?

$$M \sim 1.3 M_{\text{sun}} ; R \sim 1.5 R_{\text{sun}} ; \text{Age} \sim 3.1 \times 10^9 \text{ yr}$$

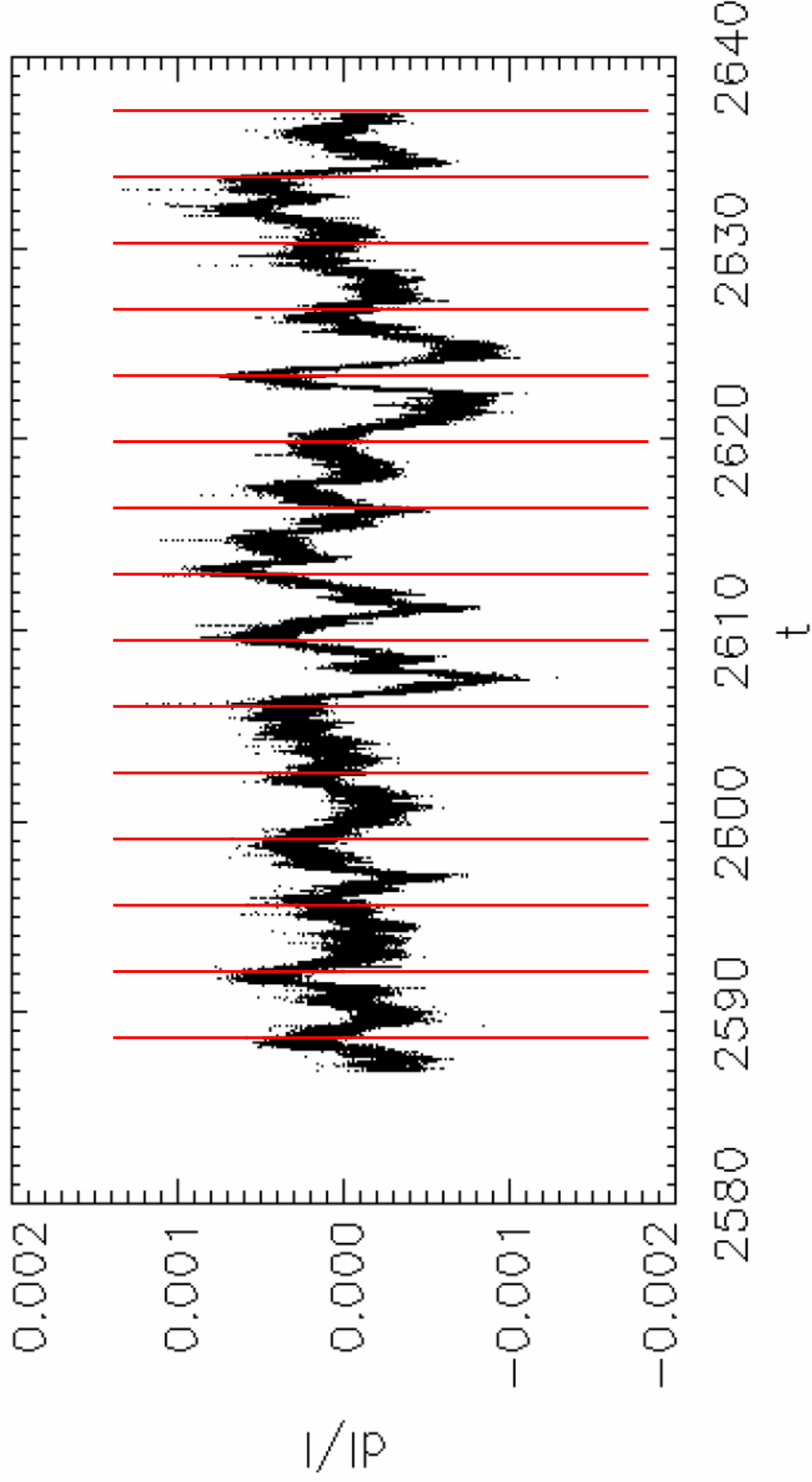
$$R/R_{\text{sun}} = 1.50$$

$$V \sin(i) = 10.9 \text{ km/s} \rightarrow P_{\text{ROT}} = 7.0 \text{ d}$$



$$P_{\text{ROT}} \approx 3.5 \text{ d}$$

$$\sin(i) \approx 0.5 \rightarrow i \approx 30^\circ$$



Typical spot size: 0.0005
Large spots: 0.0015

CoRoT: HD 49933

Typical spot size: 0.0005

Large spots: 0.0015

$$d_{spot}^2 = 0.0005 \times d_{star}^2 \rightarrow d_{spot} \sim 50000\text{km}$$

$$d_{spot}^2 = 0.0015 \times d_{star}^2 \rightarrow d_{spot} \sim 80000\text{km}$$

Same size as sunspots!

CoRoT: HD 49933

$$\Delta V_0 = 85.6 \mu\text{Hz}$$

$$\rho/\rho_{\text{sun}} = 0.402$$

$$M/M_{\text{sun}} = 1.3$$

$$R/R_{\text{sun}} = 1.5$$

$$P_{\text{ROT}} \approx 3.5 \text{ d}$$

$$i \approx 30^\circ$$

Typical spot size: 0.0005 ($D \approx 50,000 \text{ km}$)

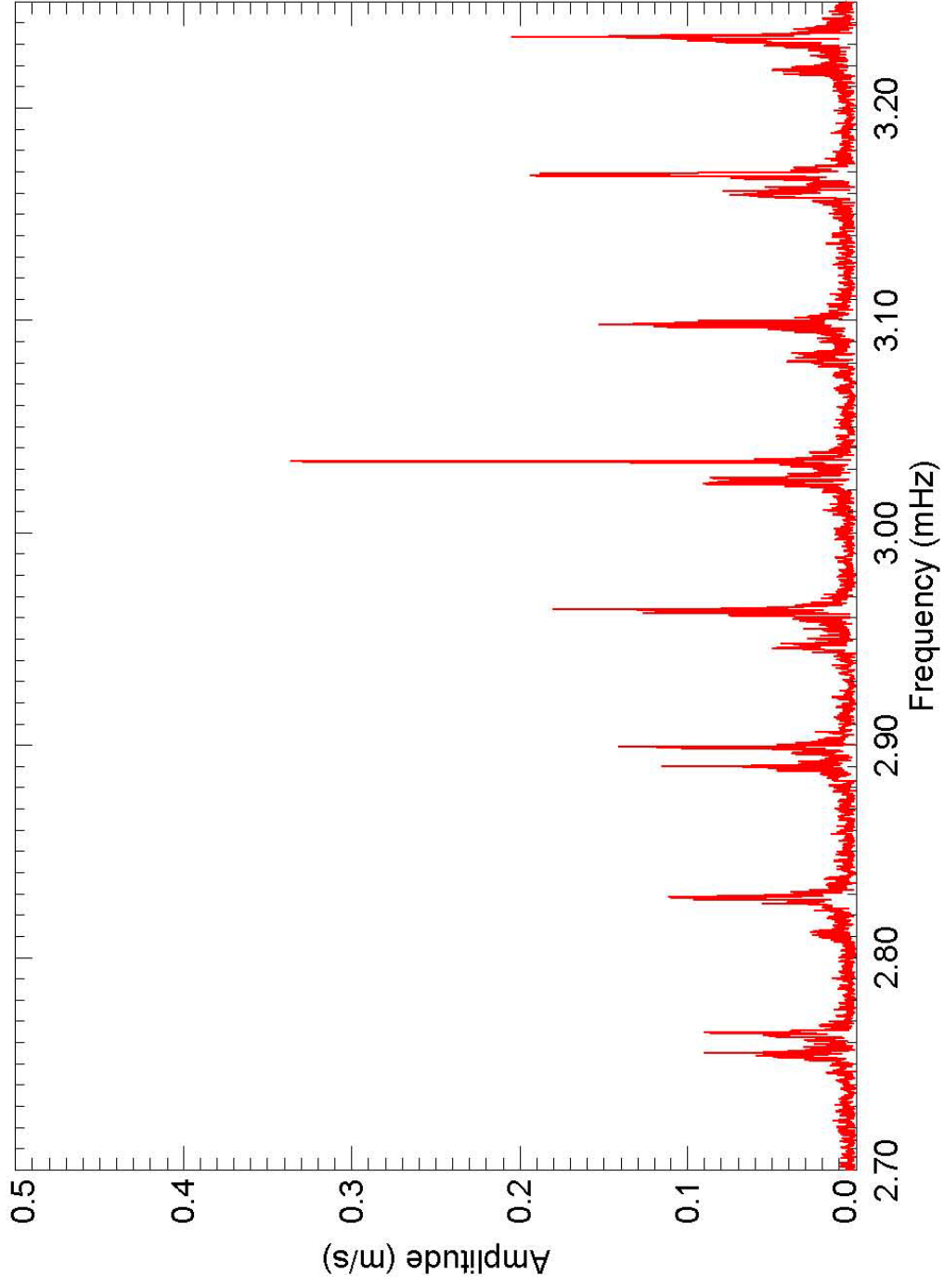
Large spots: 0.0015 ($D \approx 80,000 \text{ km}$)

$$T_{\text{eff}} = 6460 \pm 150 \text{ K}$$

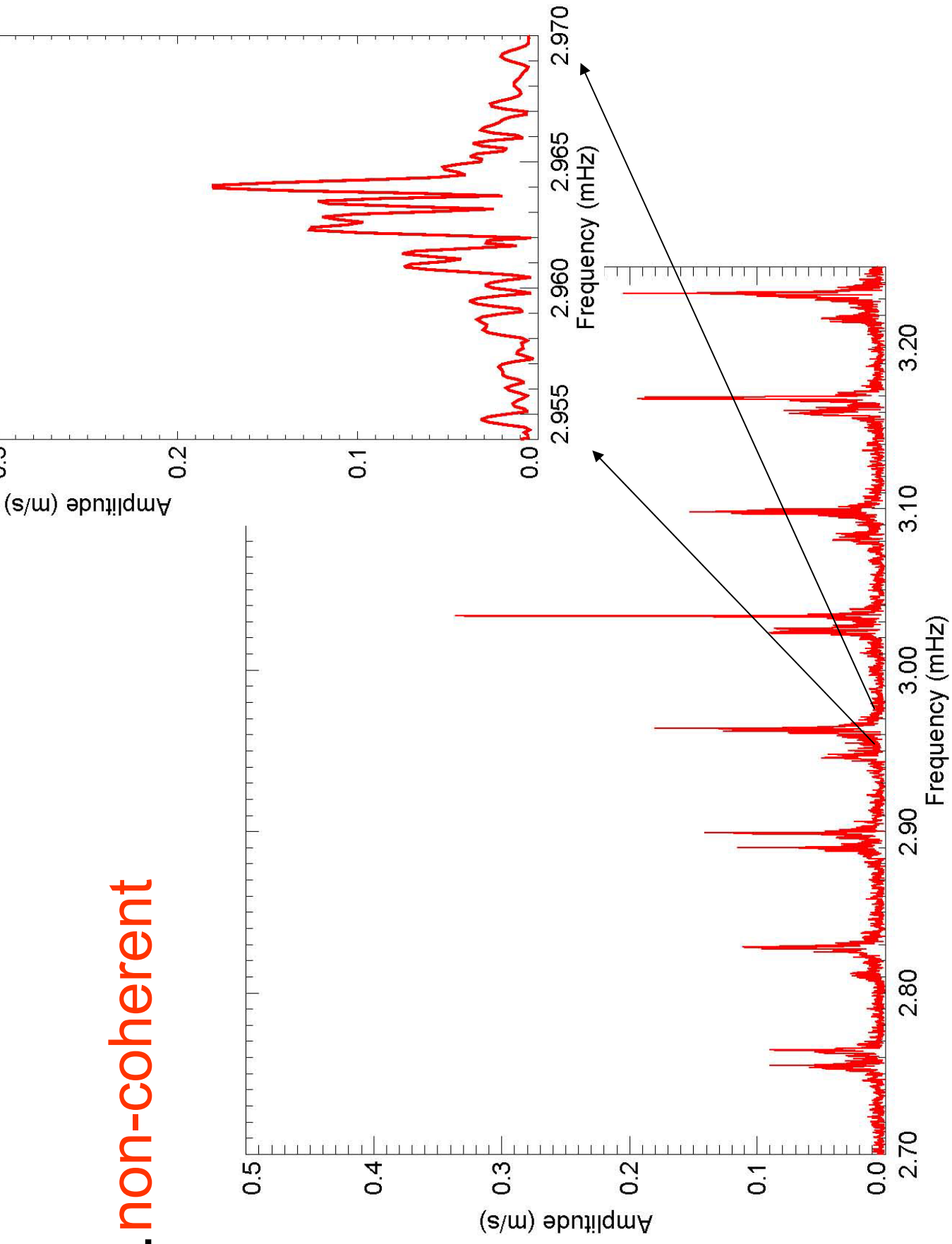
$$\text{Hipparcos: } L/L_{\text{sun}} = 3.5 \pm 0.25$$

$$R/R_{\text{sun}} = 1.50 \pm 0.09$$

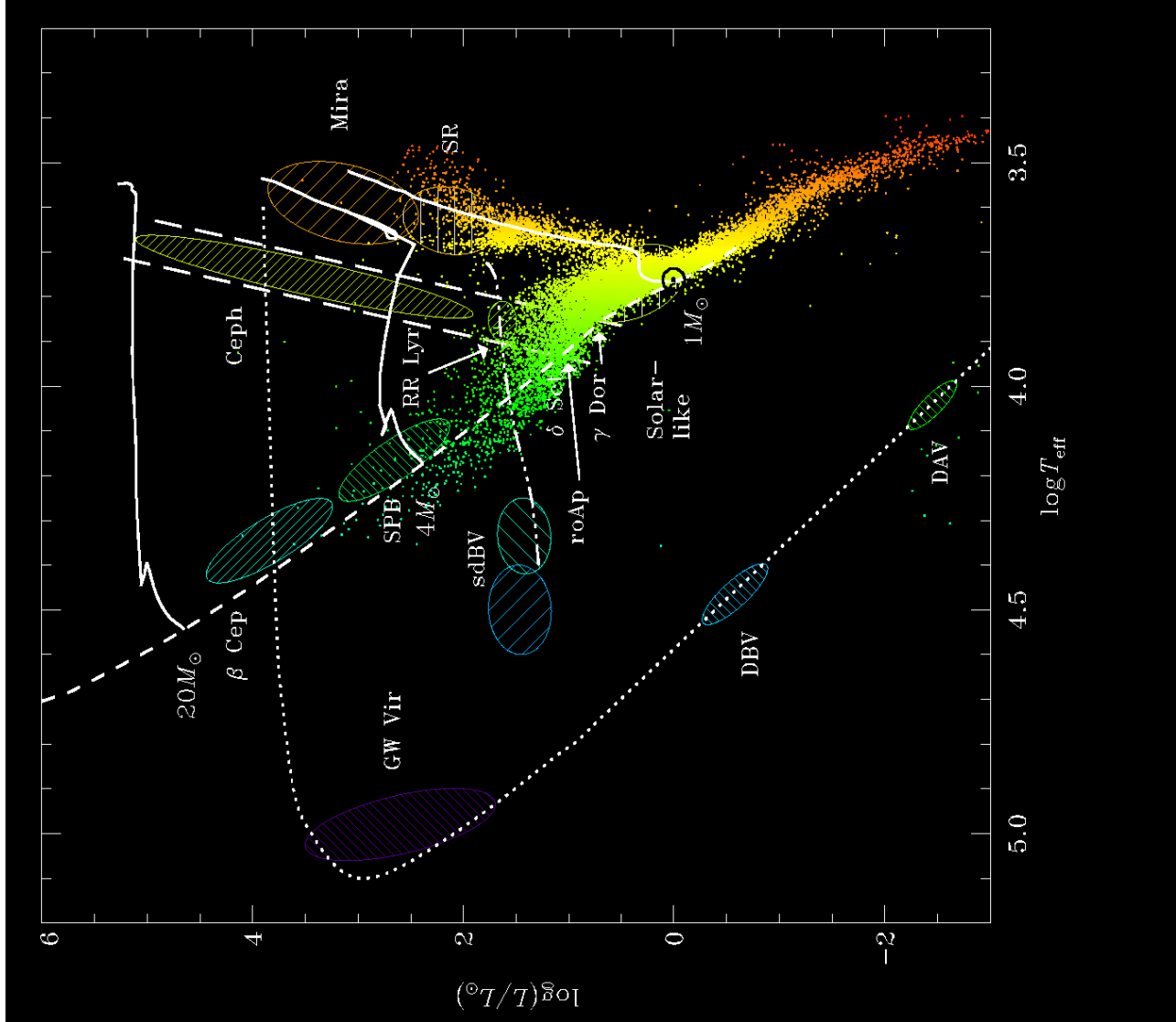
Solar-like oscillations are..



...non-coherent



The HR-diagram: Many types of pulsating stars



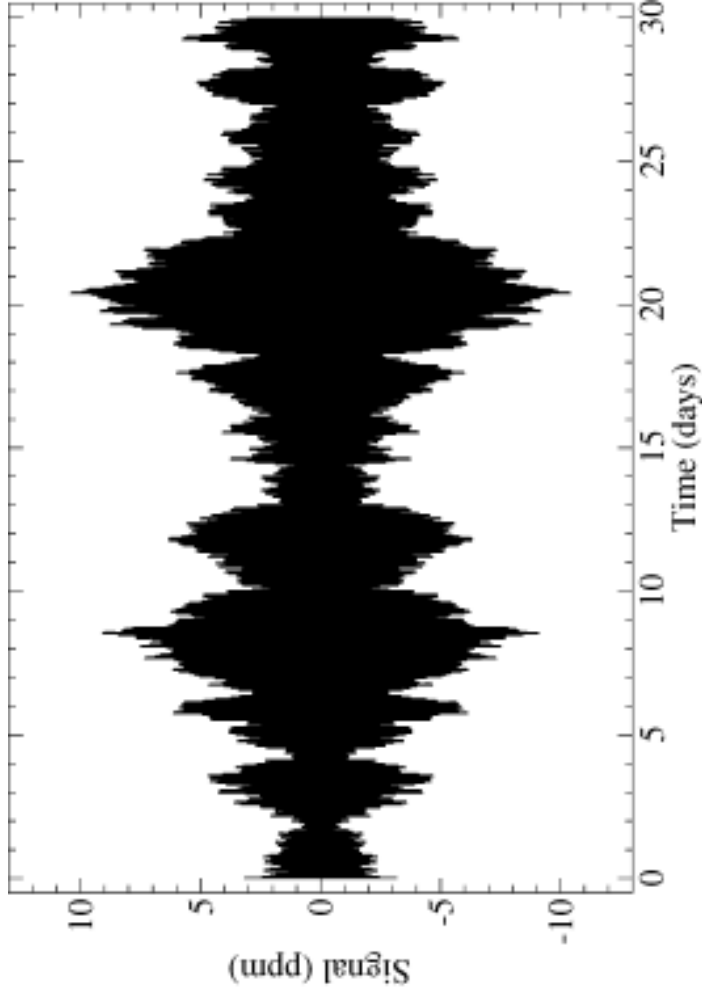
The Kappa-mechanism:

- Delta Scuti
- Beta Cepheid
- Cepheids
- RR Lyrae

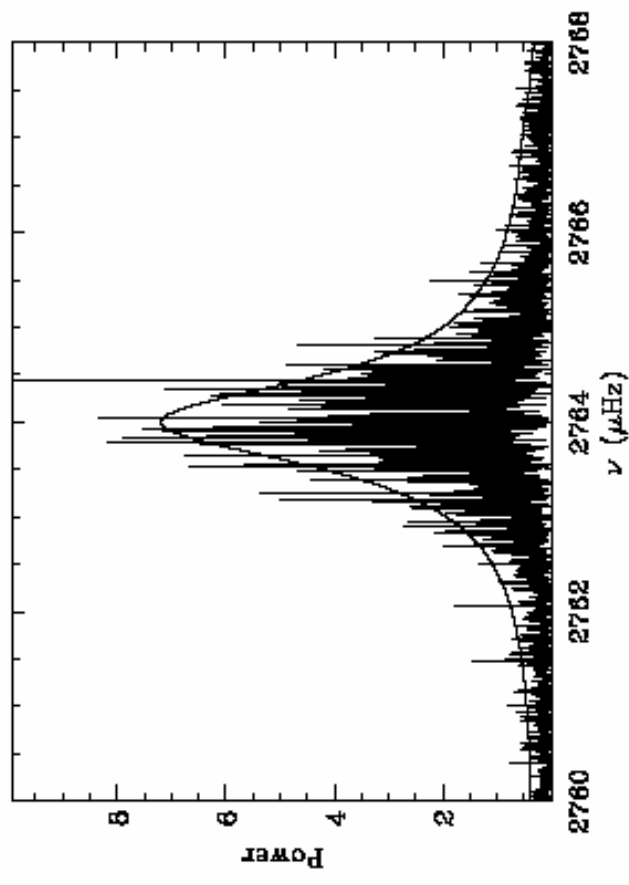
Coherent oscillations

Solar-like oscillations

- The oscillations are actually **stable modes** stochastically excited by convection
- Random excitation and exponential decay → Lorentz Profile



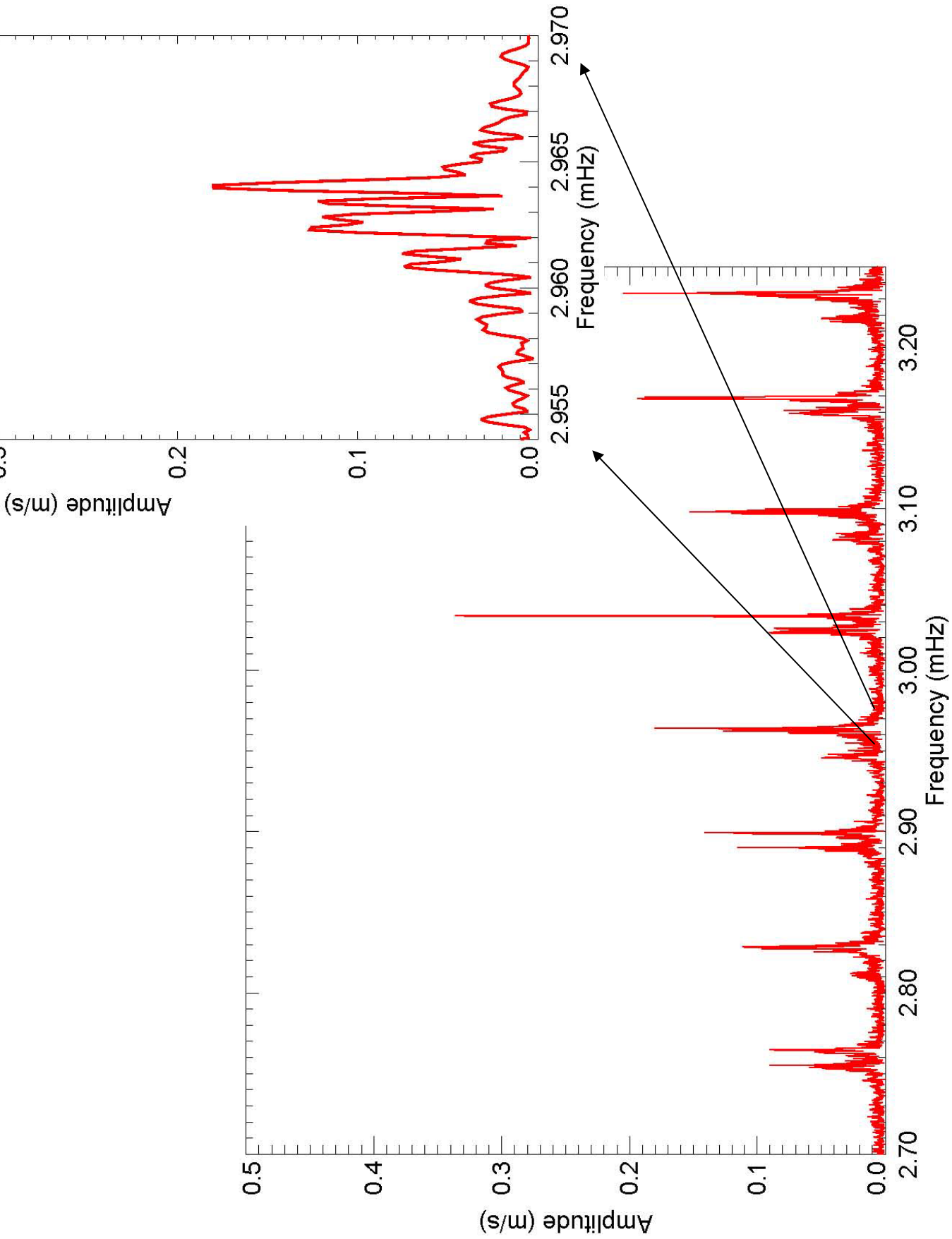
A single, stochastic mode

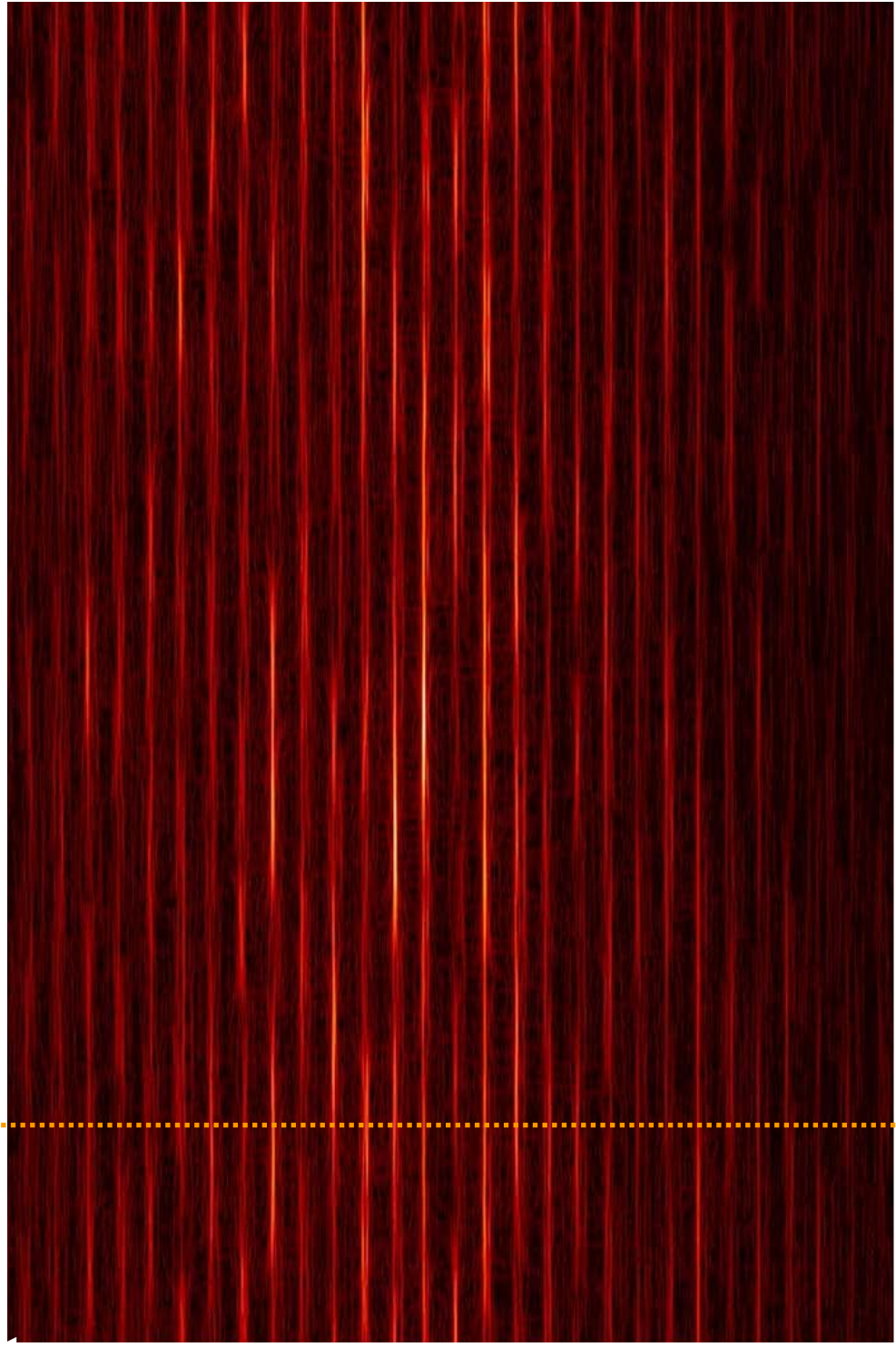


The Sun – fit multiplied by 3

Solar-like oscillations

- The width of the Lorentzian depends on the **mode lifetime**
- Typically a couple of days – but not yet well-understood
- Typically not resolved in ground-based campaigns on solar-like stars
 - requires observations over many lifetimes, which we so far only have for **the Sun**



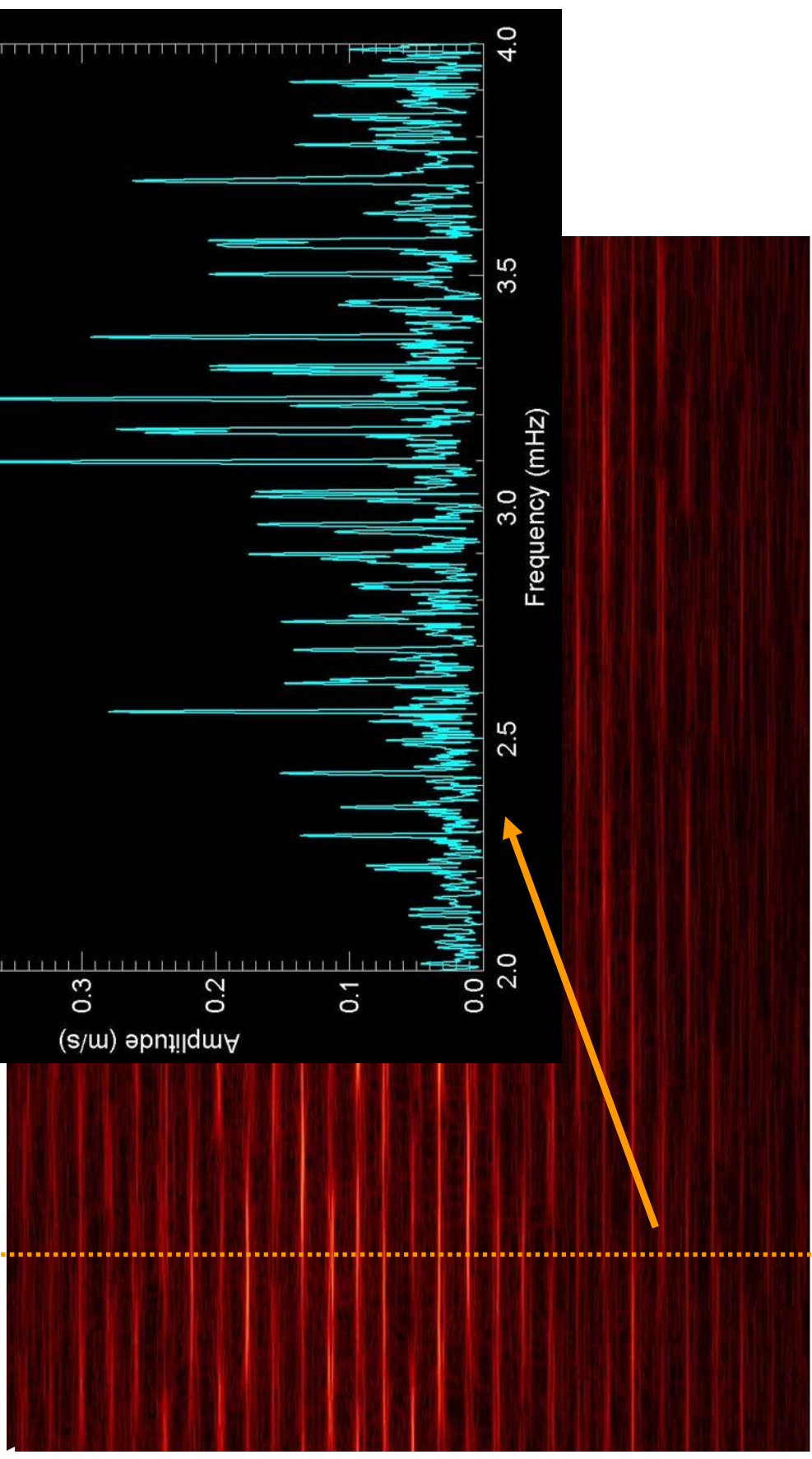


4.1 mHz

2.1 mHz

0 d

22 d



4.1 mHz

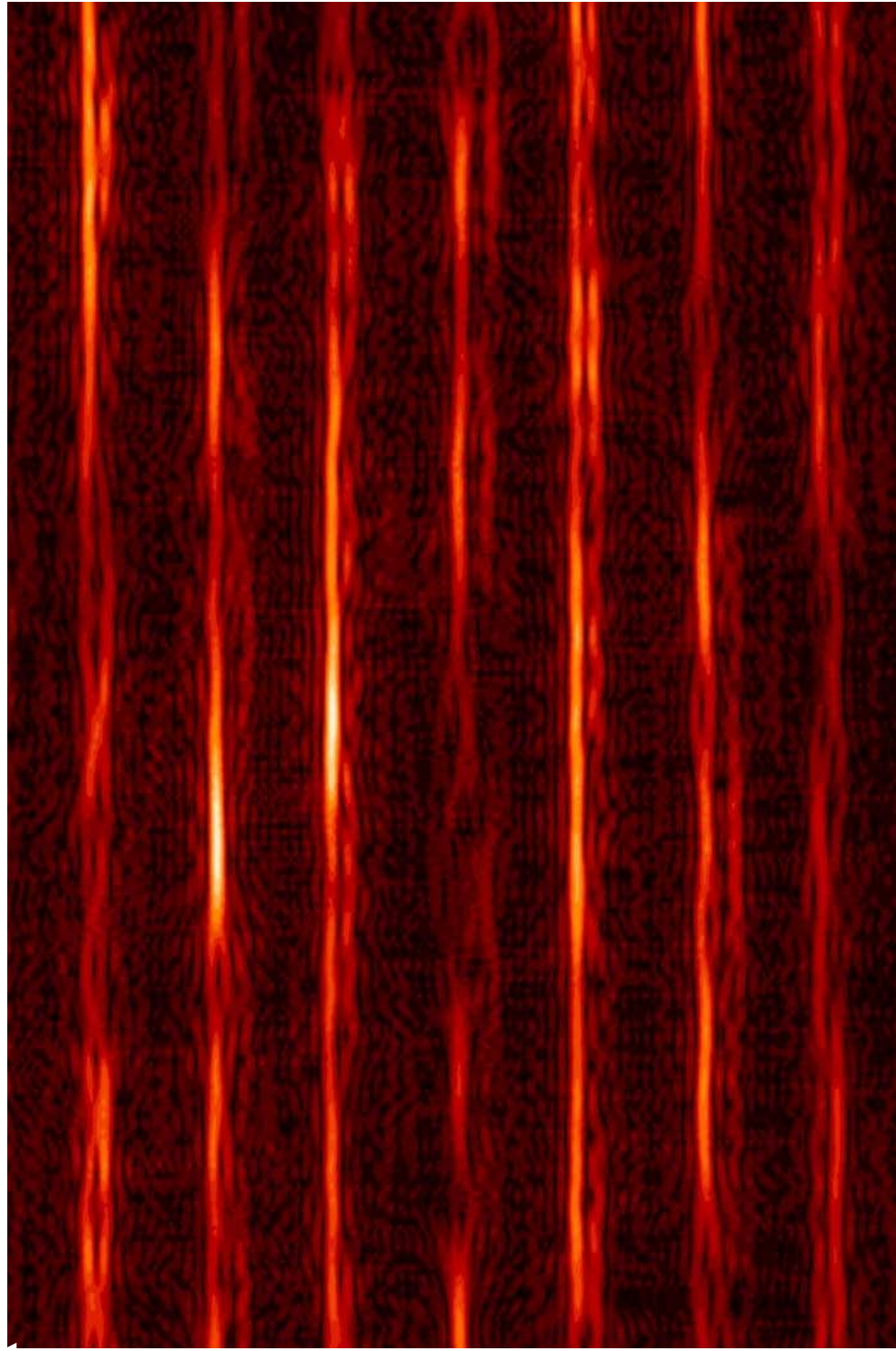
2.1 mHz

0 d

22 d

Amplitude (m/s)

Frequency (mHz)



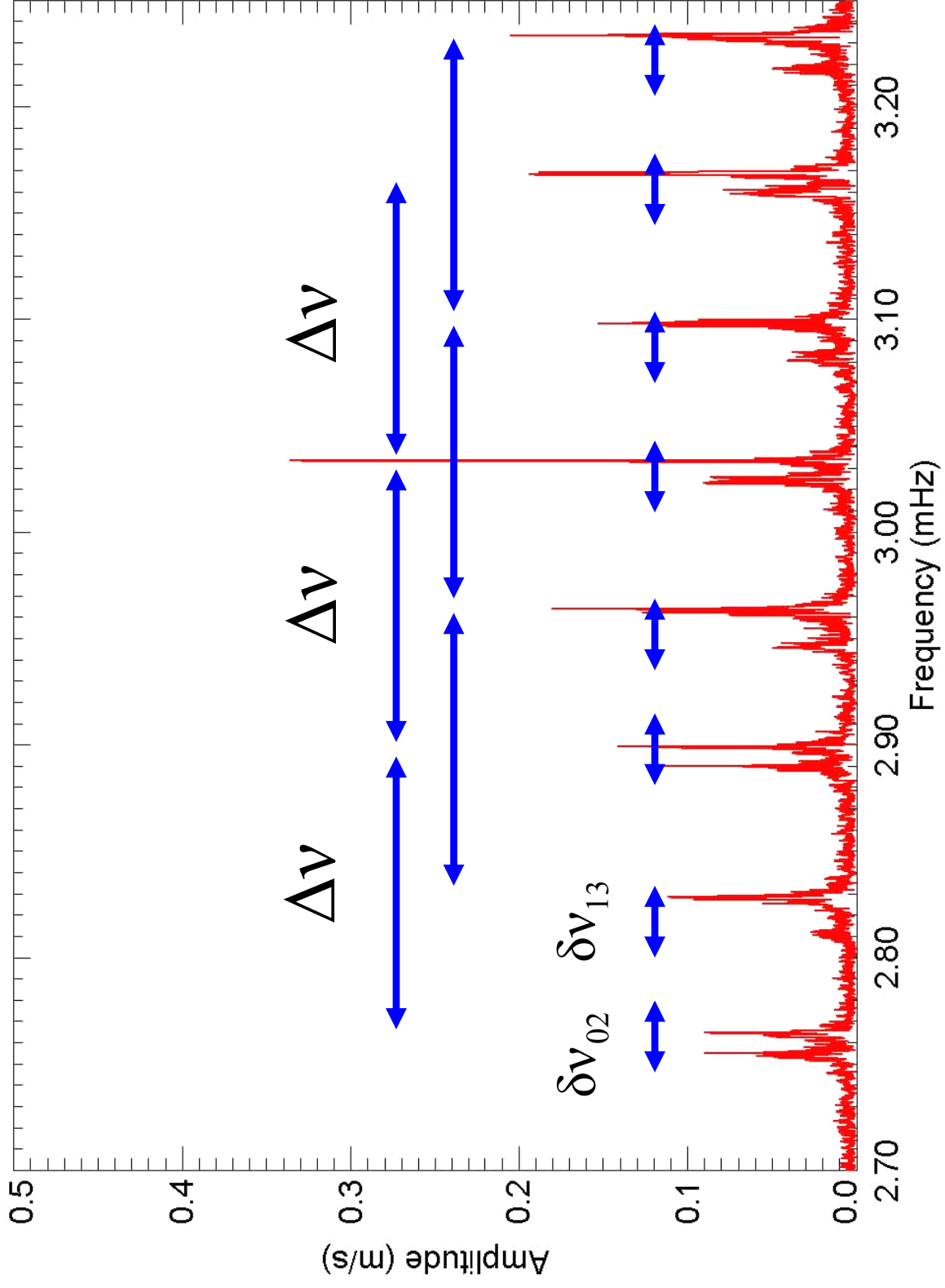
3.35 mHz

2.85 mHz

0 d

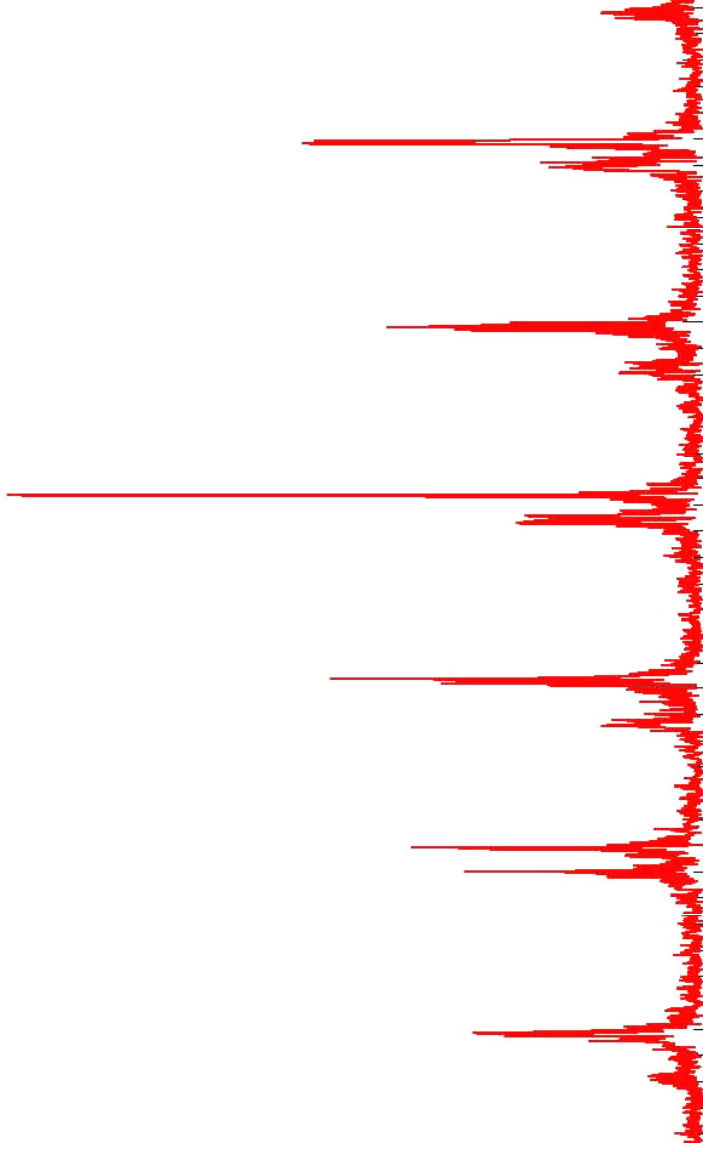
22 d

Determine the large Separation



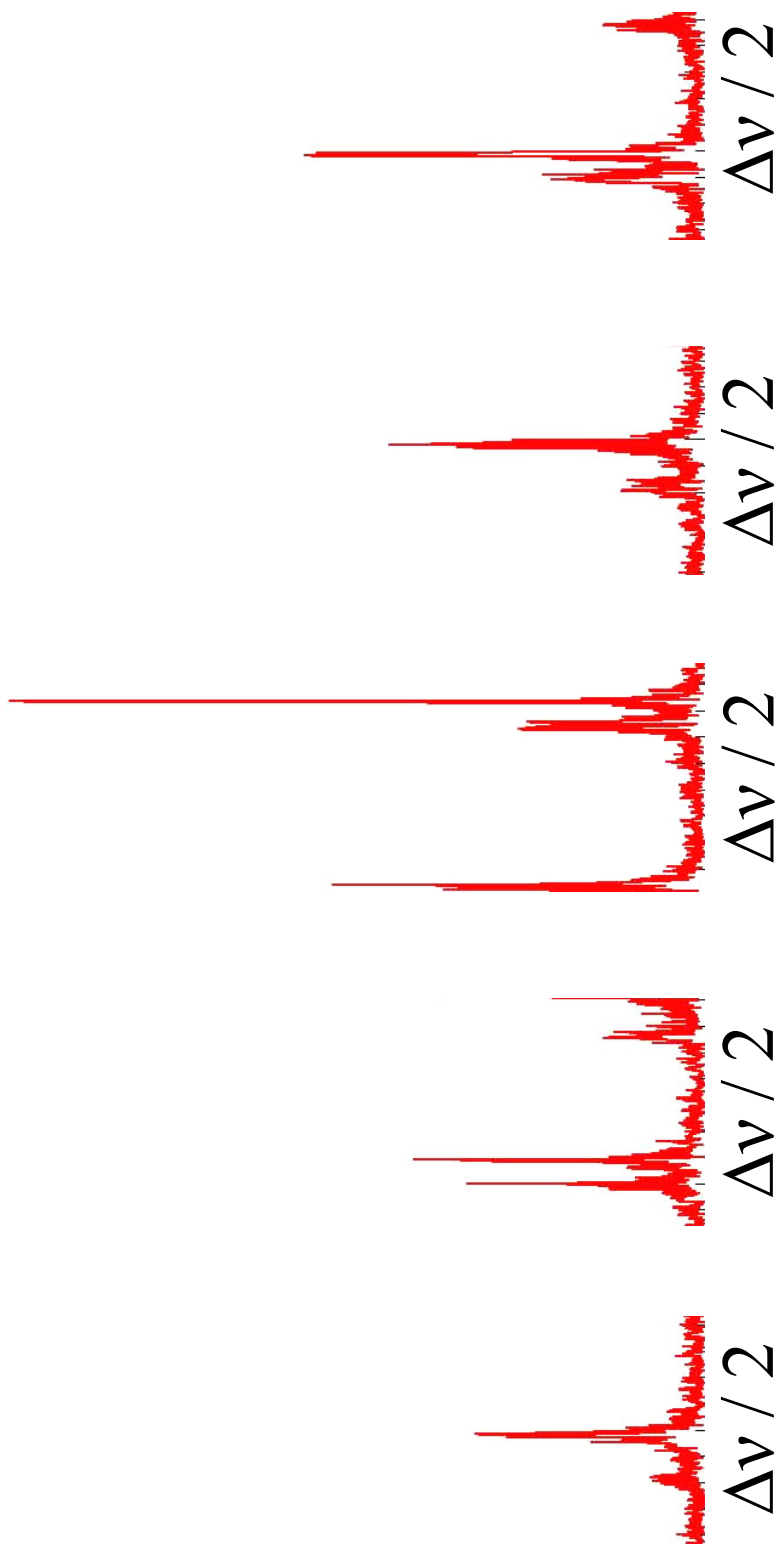
Determine the large Separation

1. Take one value for Δv (first guess)



Determine the large Separation

1. Take one value for $\Delta\nu$
2. Cut the spectrum into bins of $\Delta\nu / 2$



Determine the large Separation

1. Take one value for $\Delta\nu$
2. Cut the spectrum into bins of $\Delta\nu / 2$
3. Sum the power of each bin

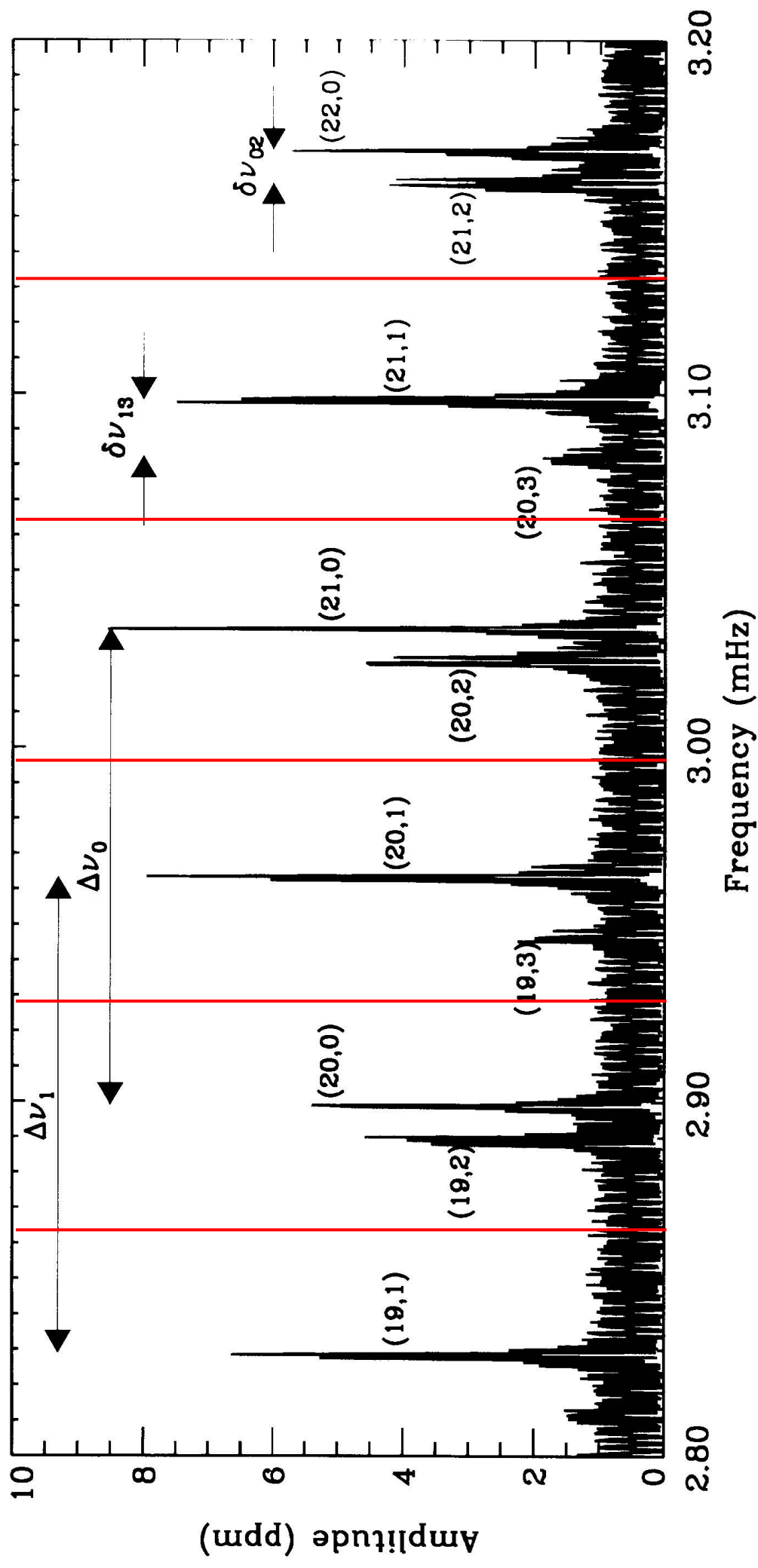


Determine the large Separation

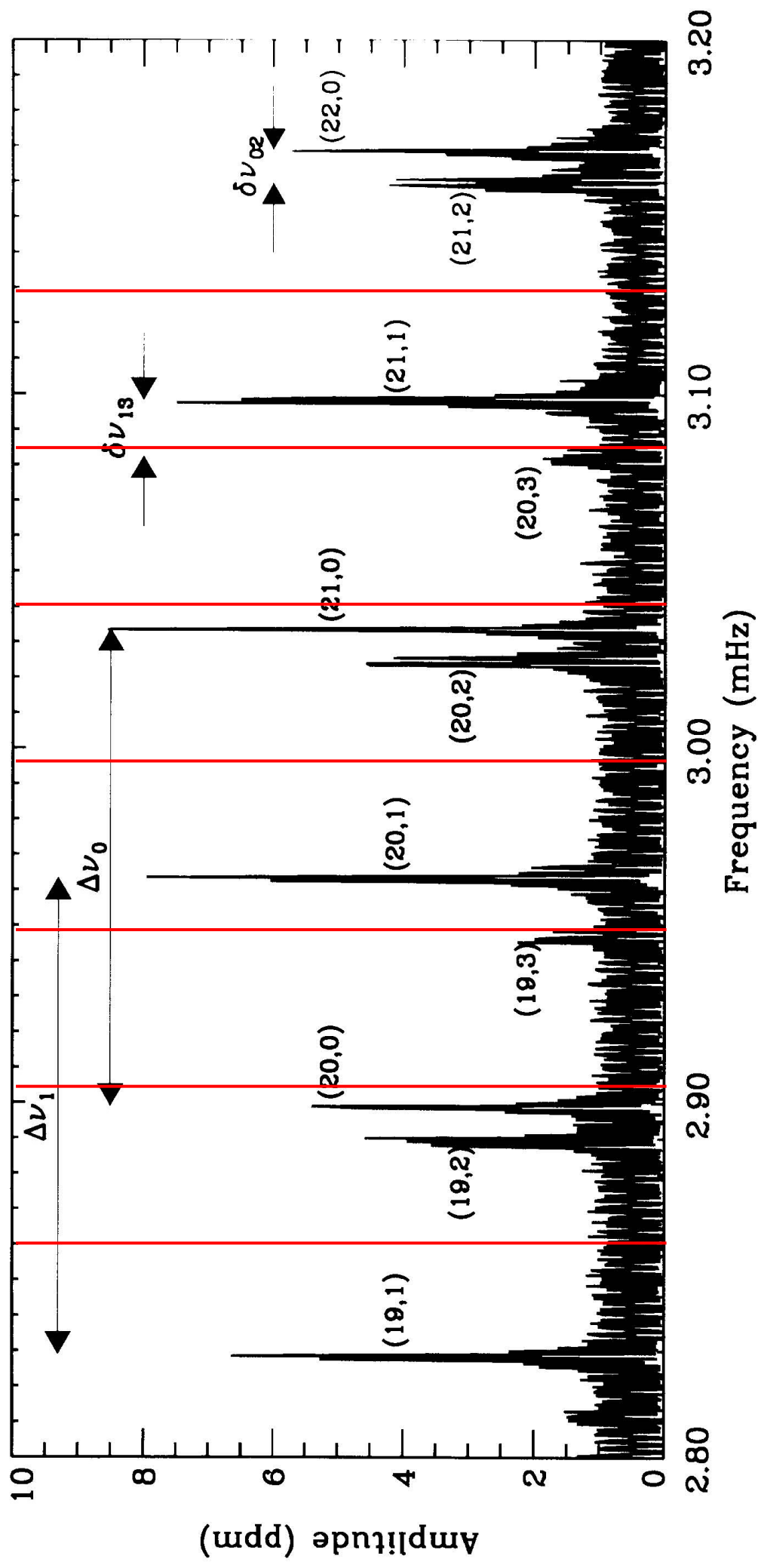
1. Take one value for $\Delta\nu$
2. Cut the spectrum into bins of $\Delta\nu / 2$
3. Sum the power of each bin
4. Find the peak of the summed power



Correct value: $l=0,1$ same position in each bin

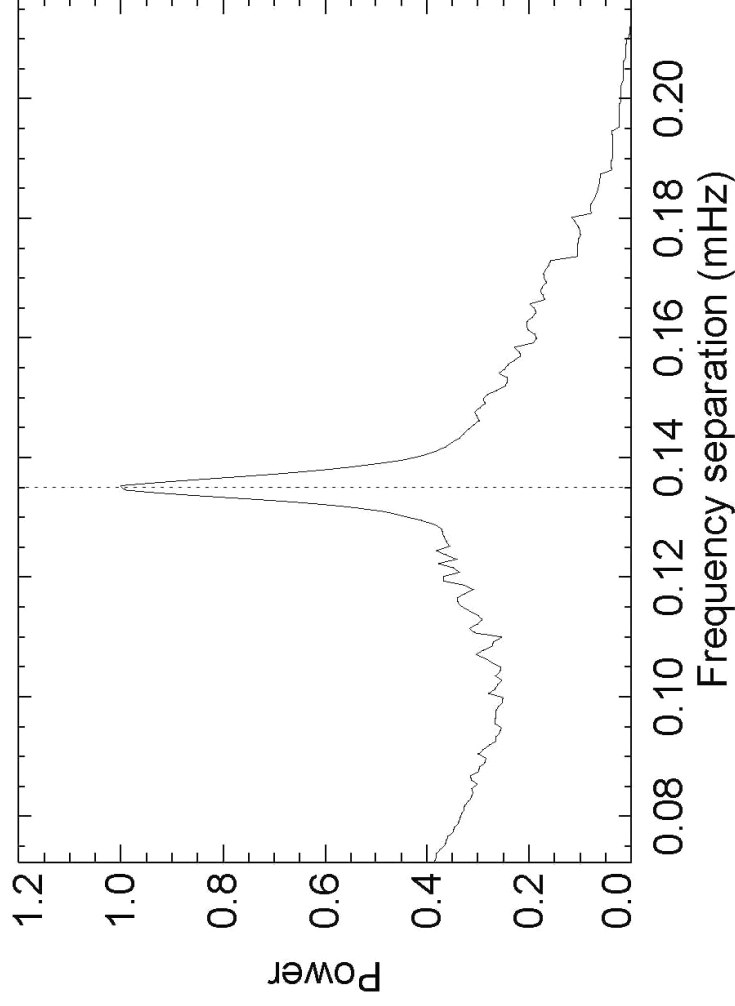


Wrong Large Separation



Determine the large Separation

1. Take one value for $\Delta\nu$
2. Cut the spectrum into bins of $\Delta\nu / 2$
3. Sum the power of each bin
4. Find the peak of the summed power
5. Try for all possible values of $\Delta\nu$



Extract the frequencies (using iterative fitting):

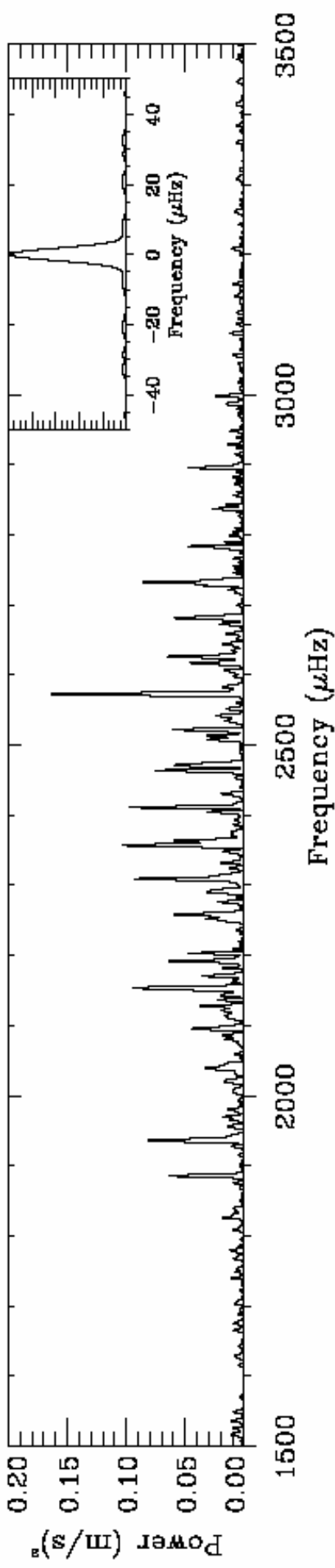


TABLE 1

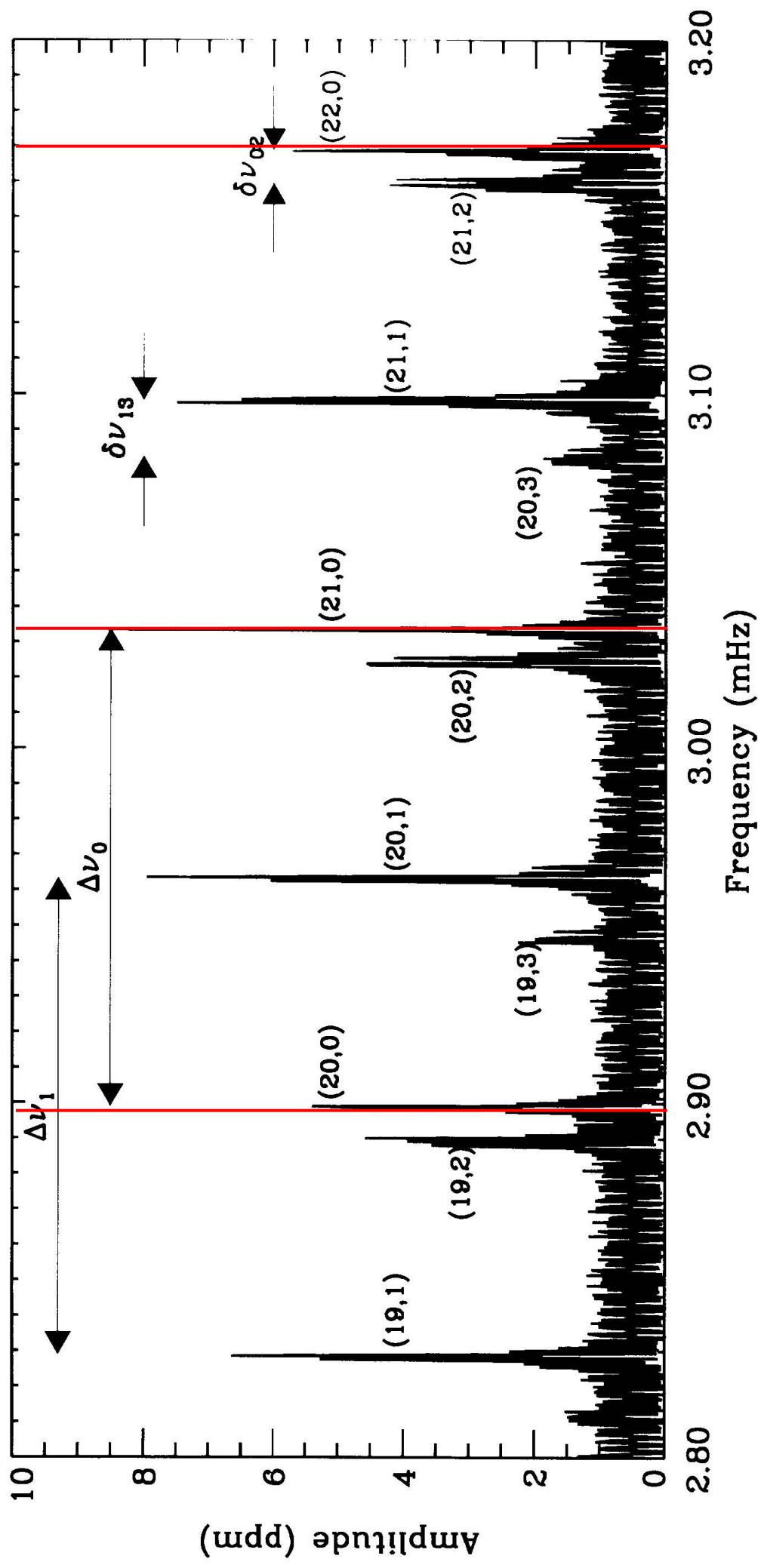
OSCILLATION FREQUENCIES FOR α CEN A (μHz)

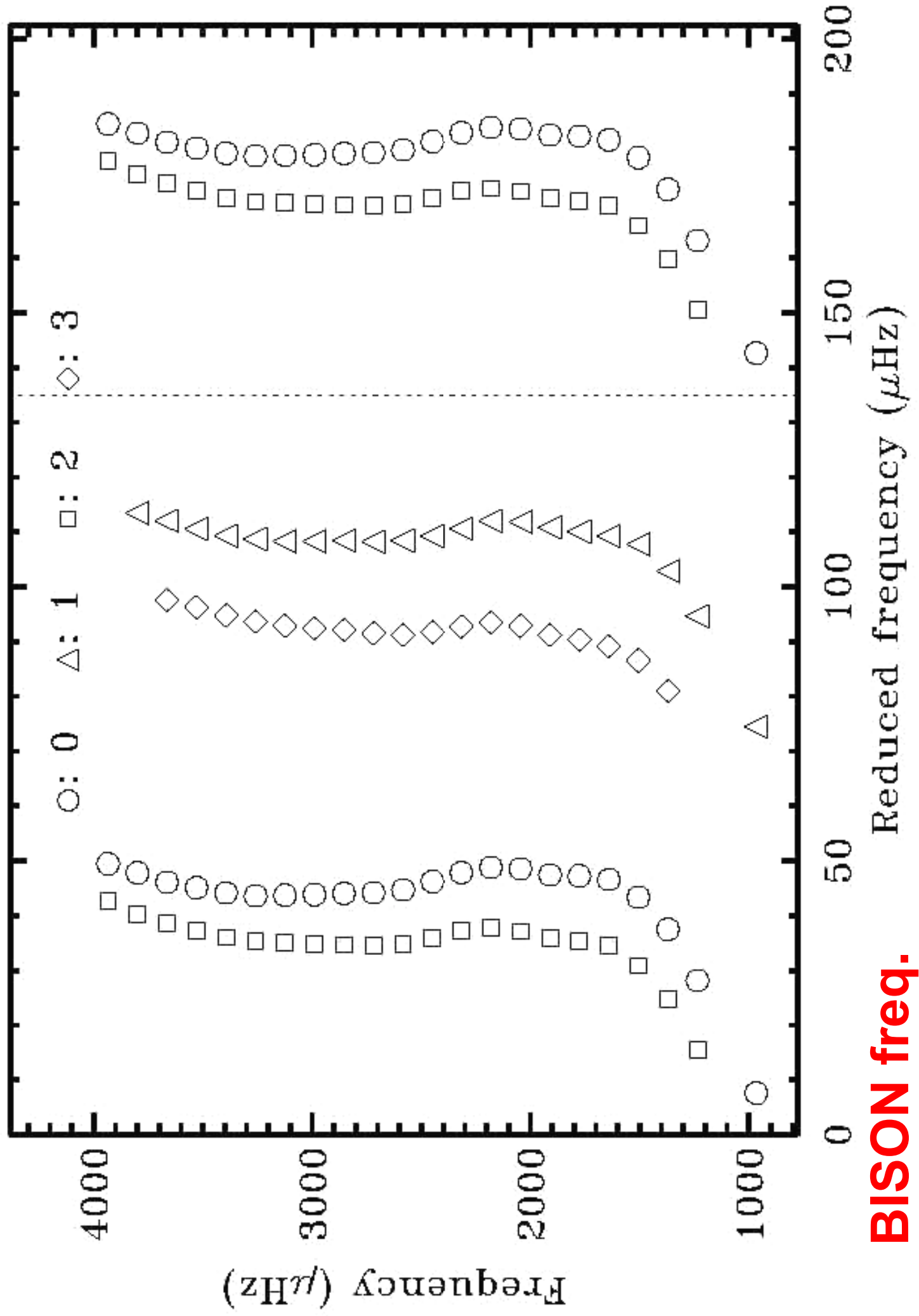
n	$l = 0$	$l = 1$	$l = 2$	$l = 3$
14.....	...	1675.9
15.....	...	1779.7	1828.6	...
16.....	1839.2	1885.9	1935.7	...
17.....	1943.3	1993.8	2038.9	2082.9
18.....	2045.5	2094.6	2146.3	2193.1
19.....	2152.9	2203.2	2253.4	2296.3
20.....	2258.1	2309.1	2357.3	2404.8
21.....	2364.0	2412.4	2463.4	2507.5
22.....	2471.5	2522.1	2572.7	2616.8
23.....	2572.7	2627.1	2676.8	2723.5
24.....	2682.7	2733.2	2783.4	...
25.....	...	2840.2
26.....	2895.9	2945.7	2998.3	...
27.....	...	3055.1

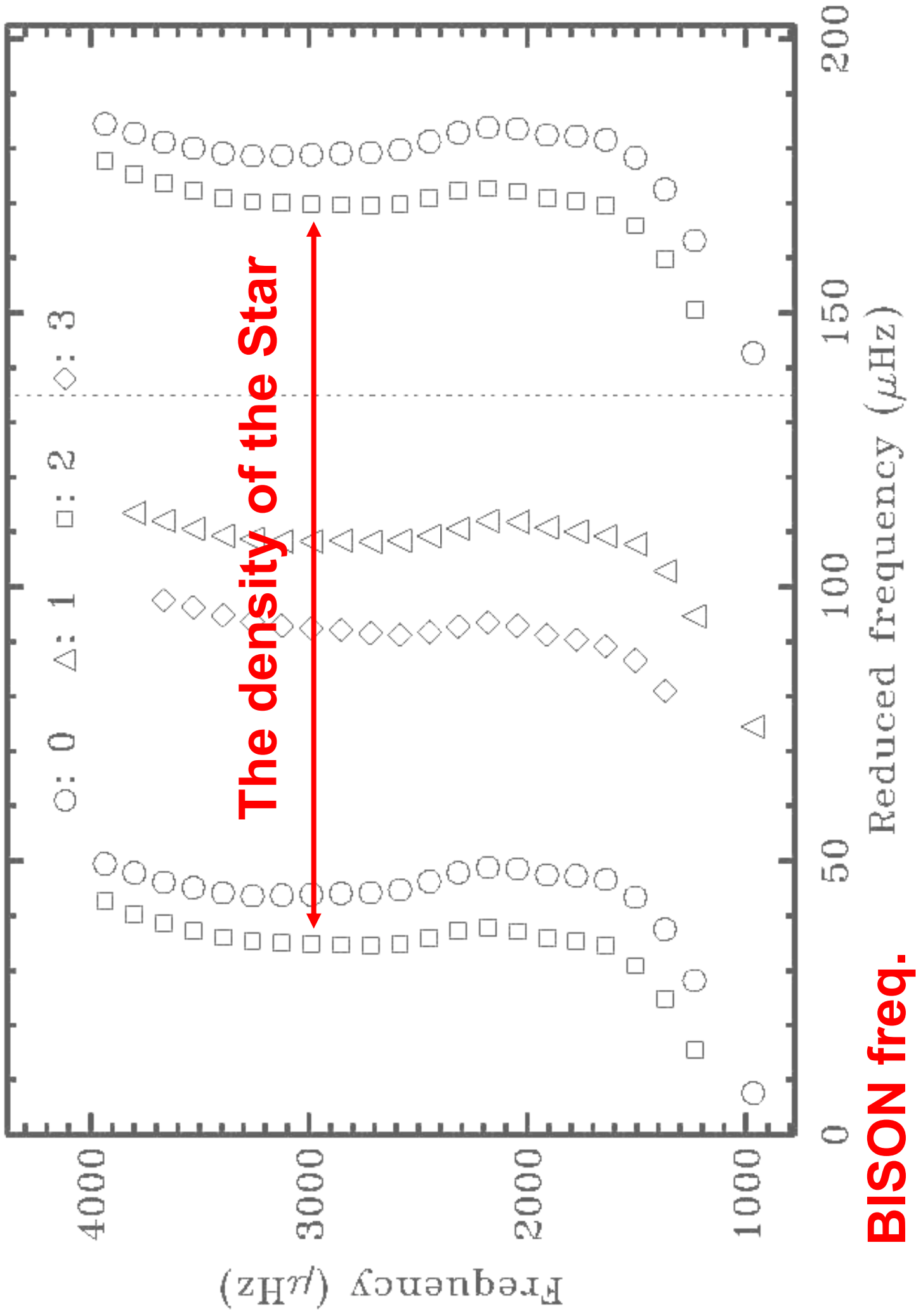
And calculate

$$\nu \bmod \Delta \nu_0$$

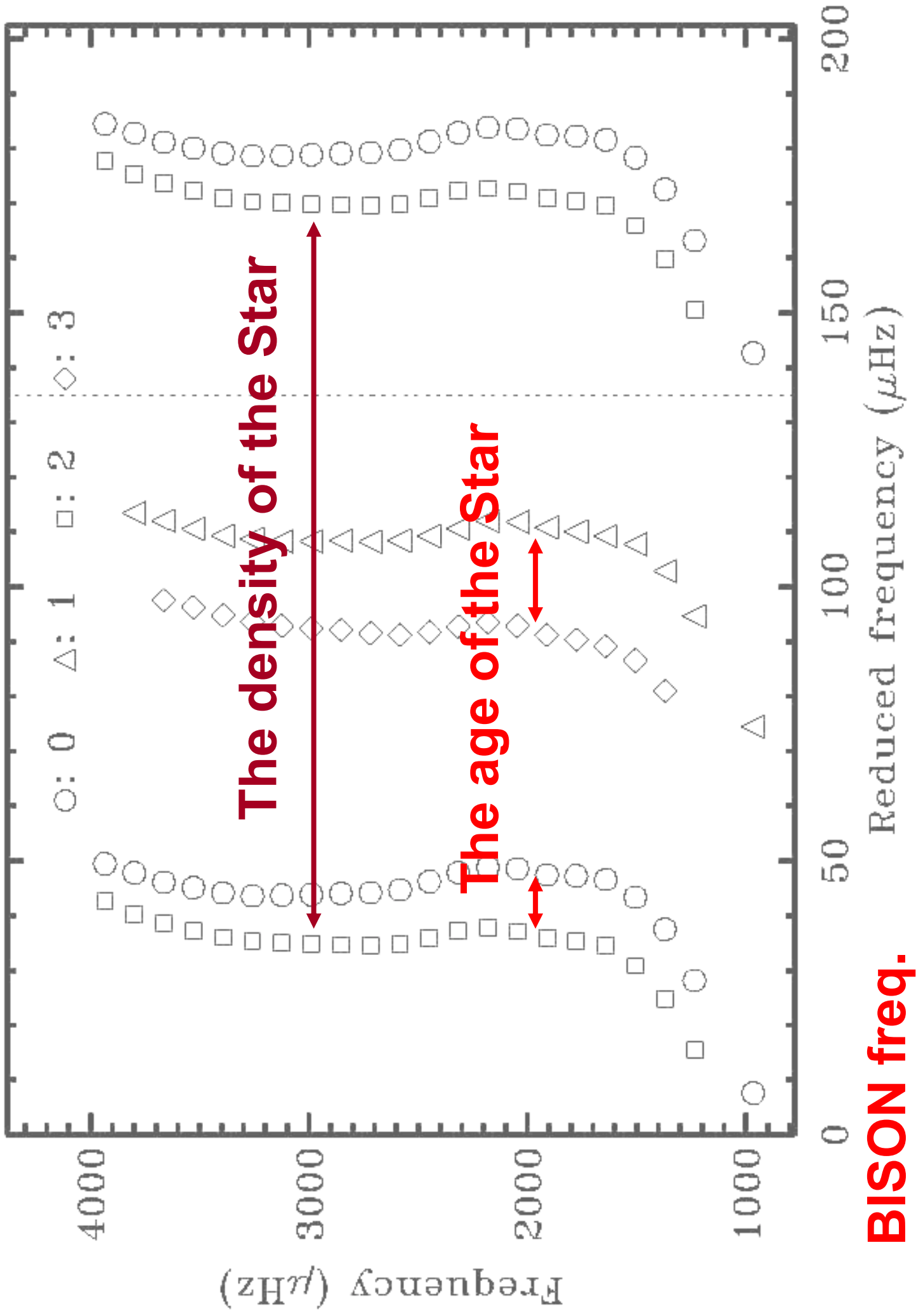
$\nu \bmod \Delta\nu_0 \sim \text{constant}$ for modes of same l



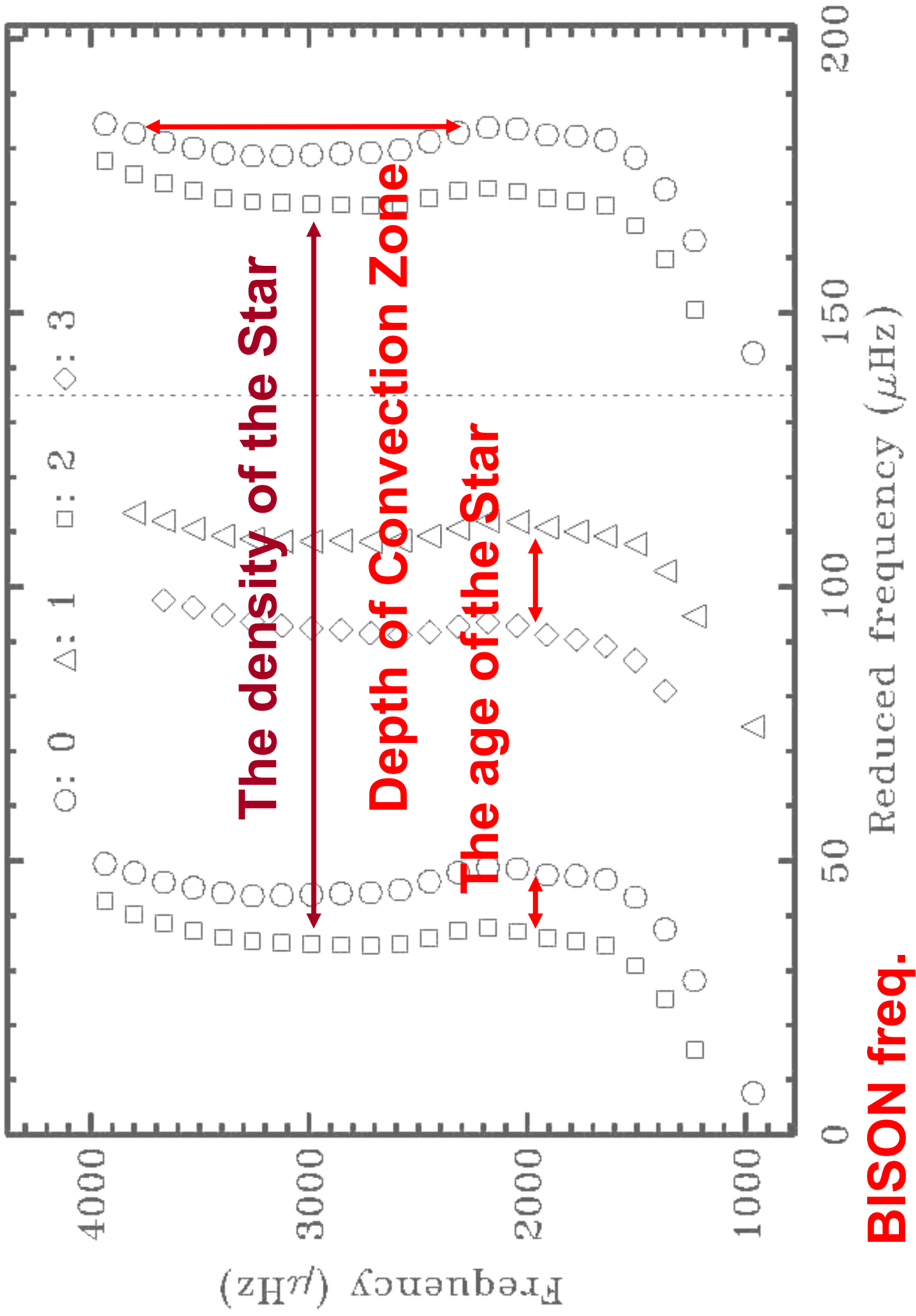




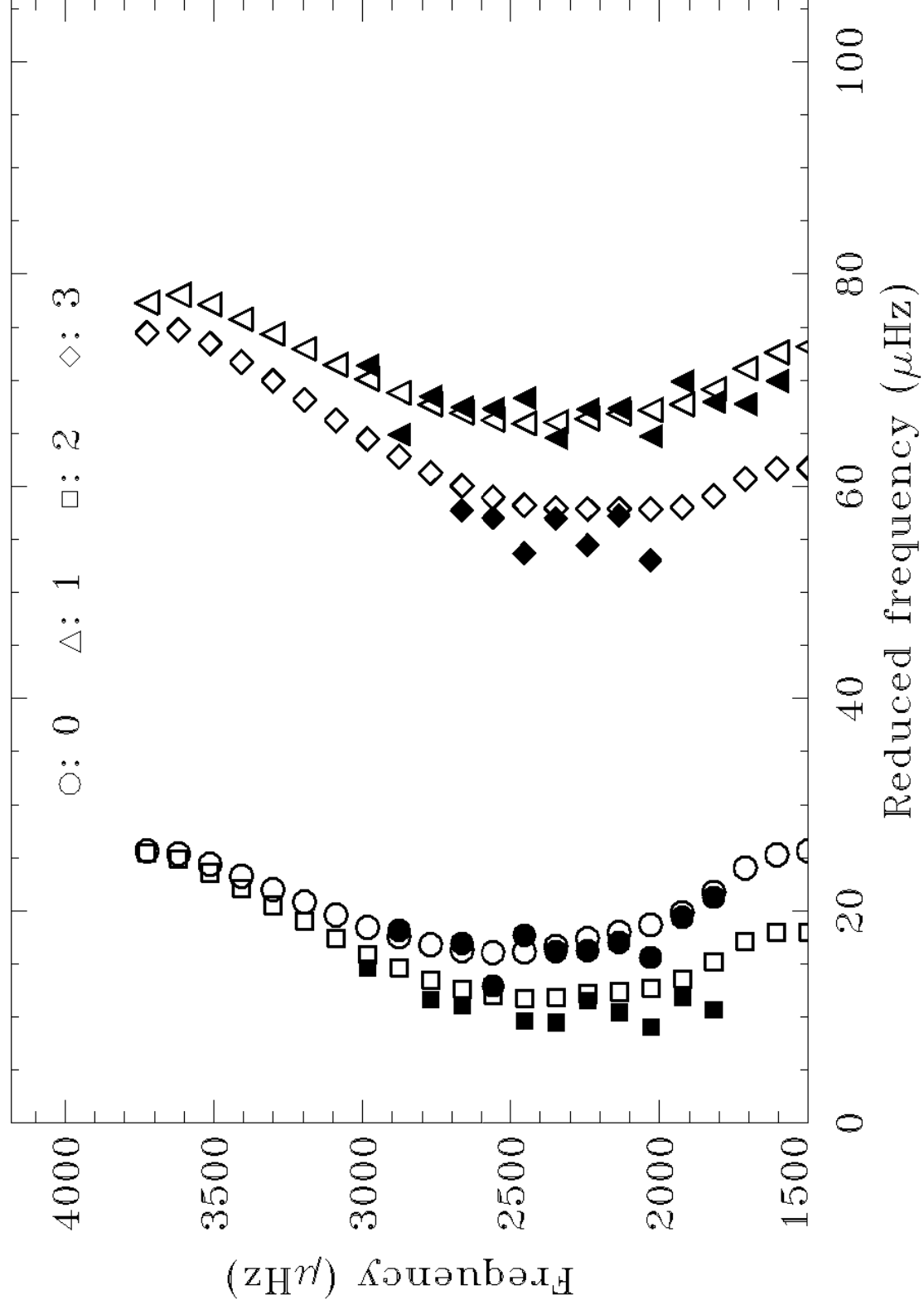
BISON freq.



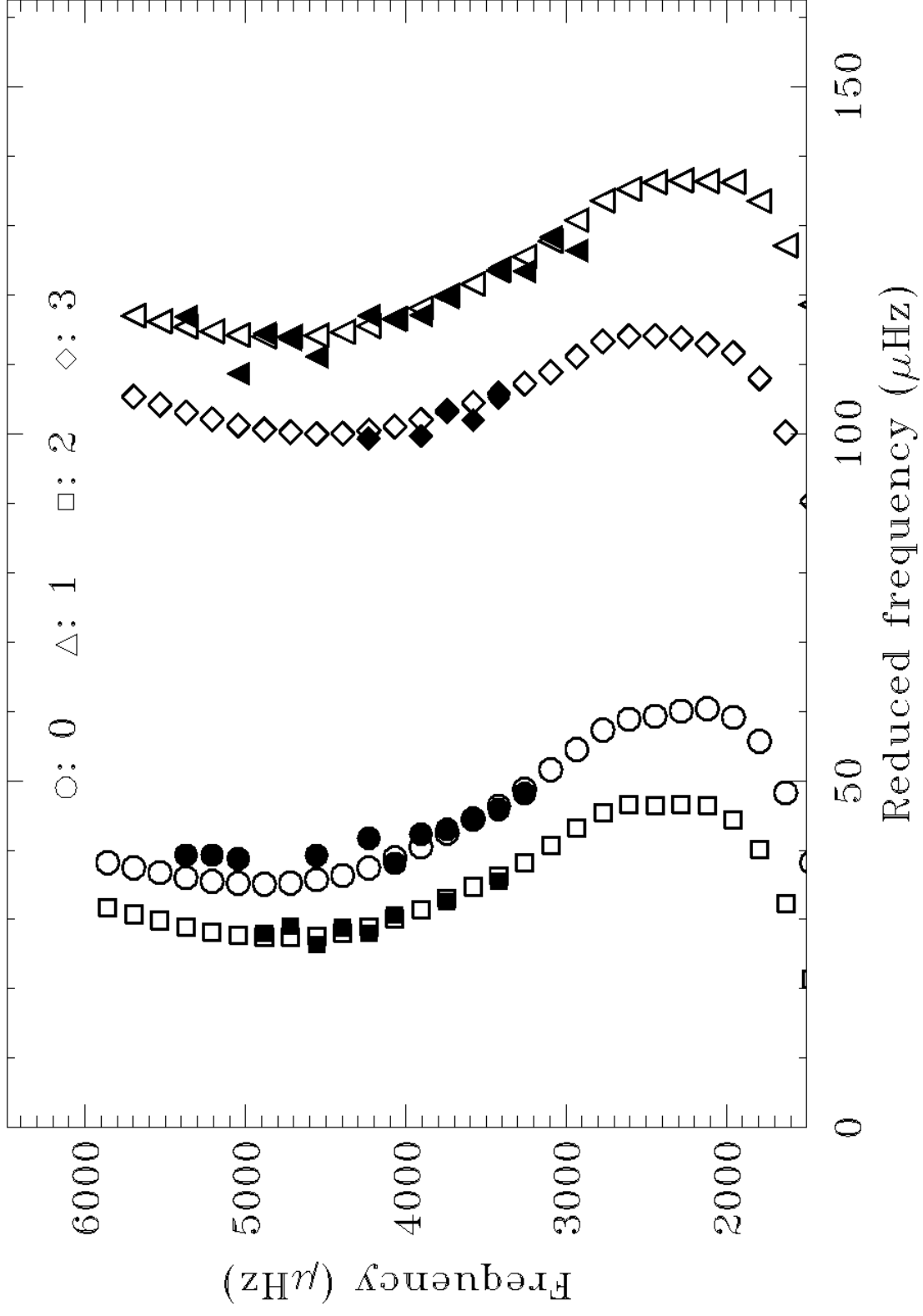
BISON freq.



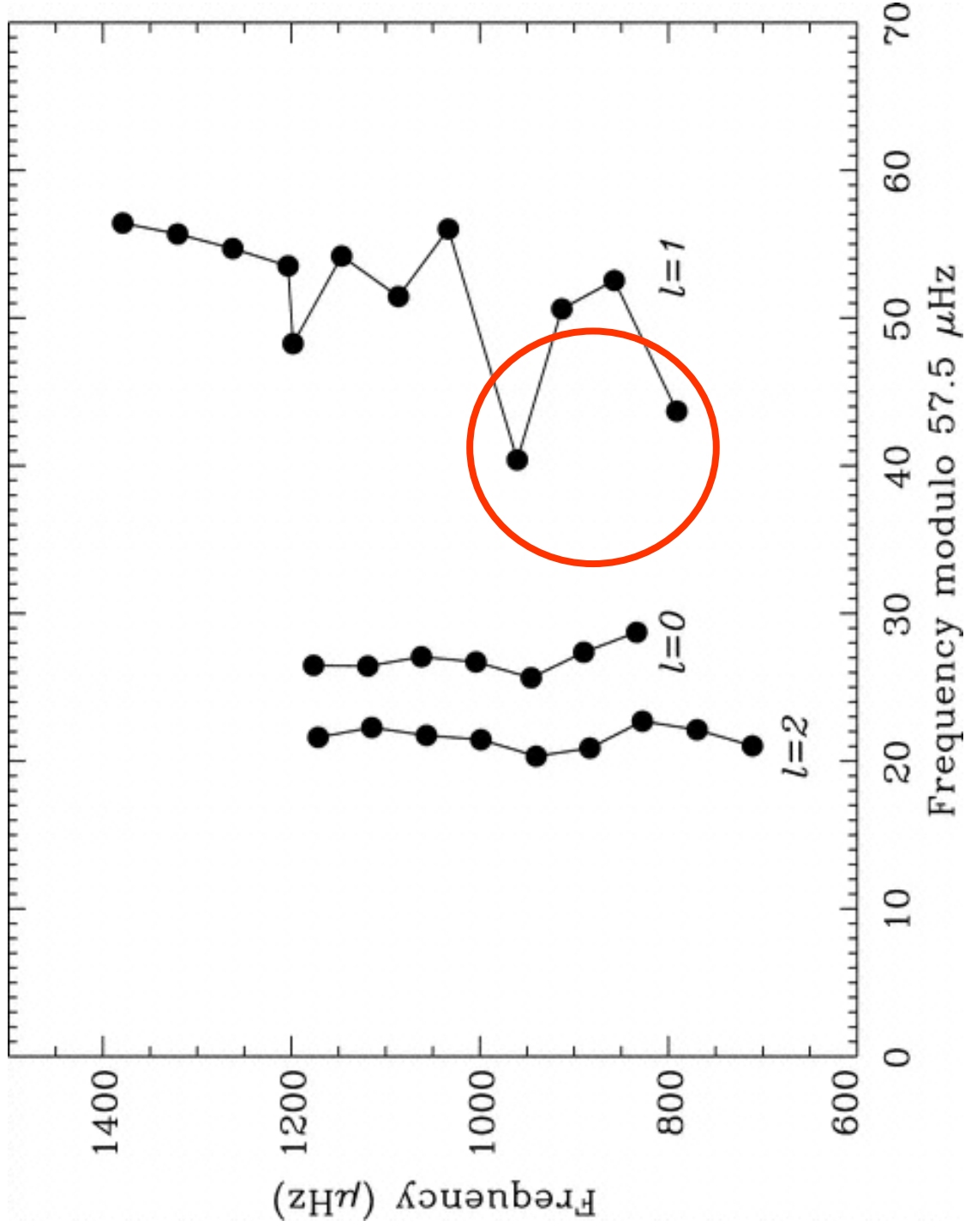
α Centauri A



α Centauri B



Beta Hydri – an evolved star:

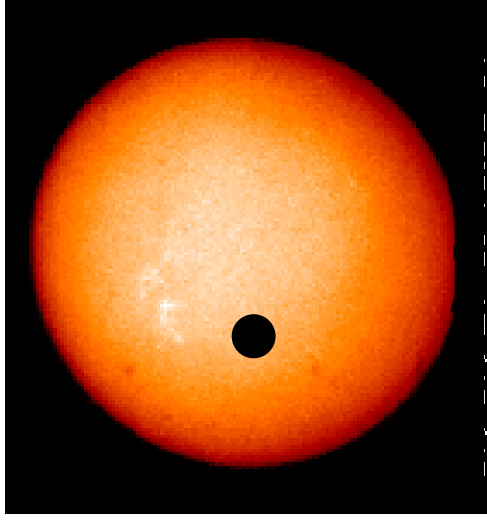


NASA Kepler mission – Launch date: 1. November 2008

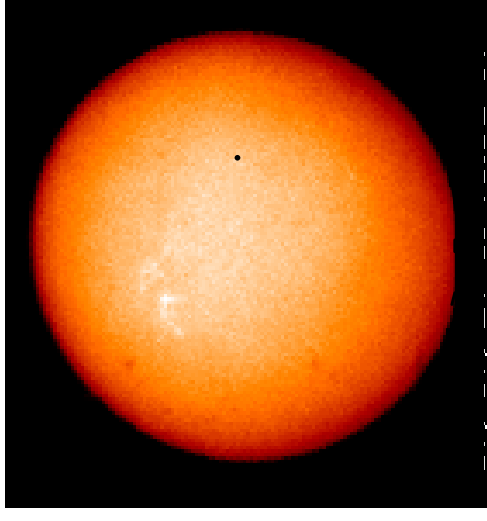


USING PHOTOMETRY TO DETECT EARTH-SIZE PLANETS

- The relative change in brightness (dL/L) is equal to the relative areas ($A_{\text{planet}}/A_{\text{star}}$)



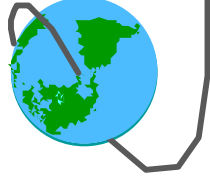
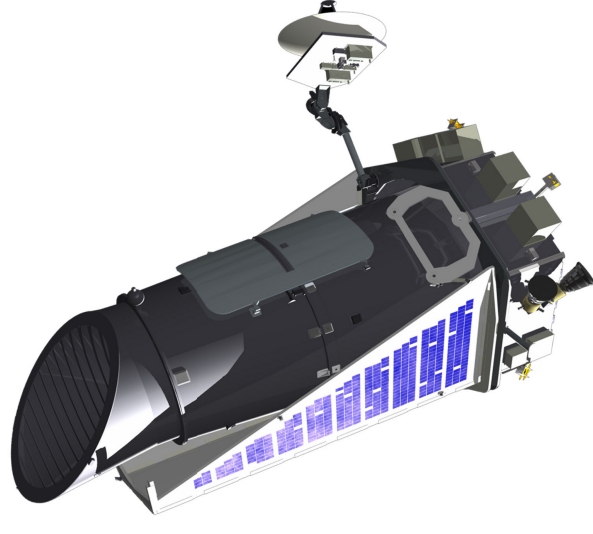
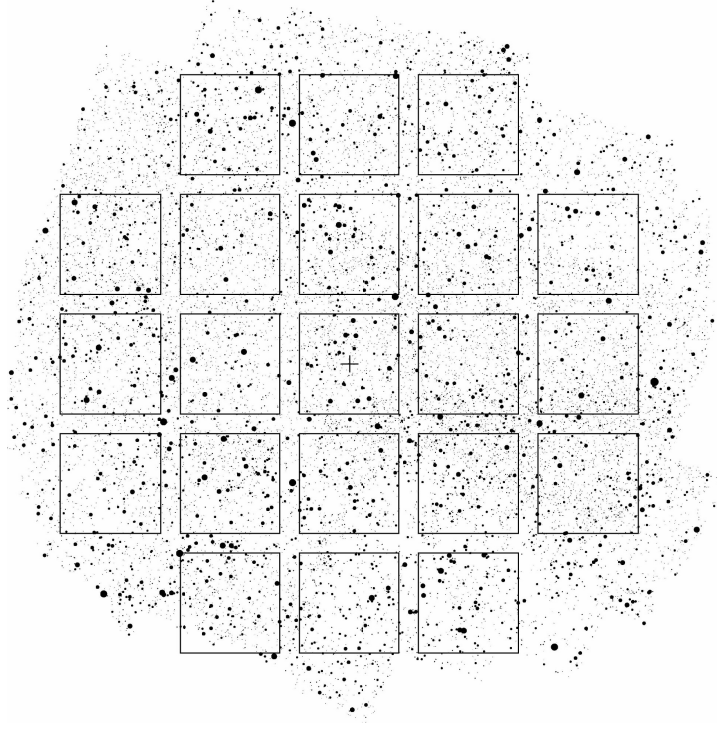
Jupiter:
1% area of the Sun (1/100)



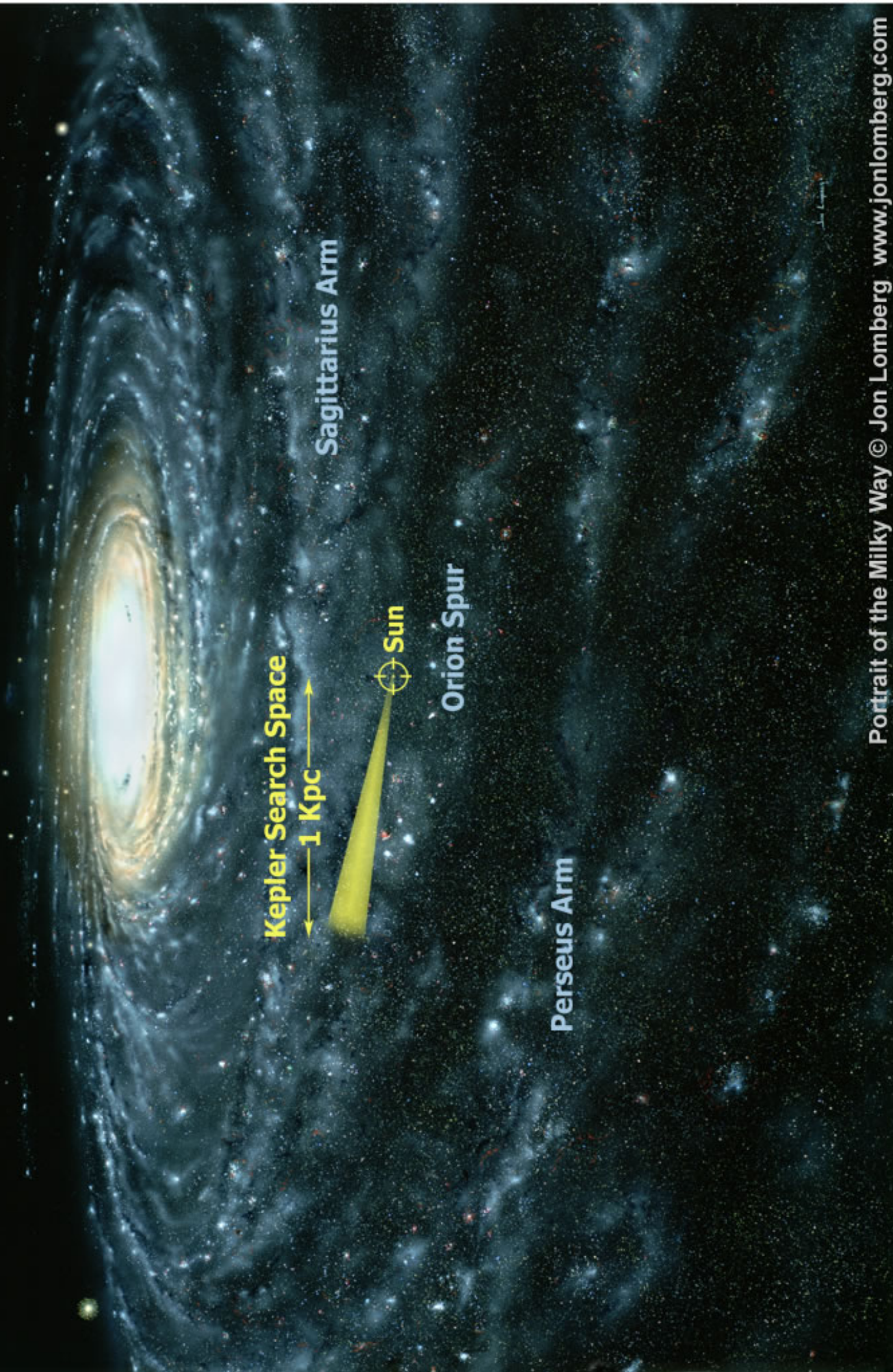
Earth or Venus
0.01% area of the Sun (1/10,000)

- To measure 0.01% must get above the Earth's atmosphere
Require at least **3 transits preferably 4** with same brightness change, duration and temporal separation

- *Kepler* is optimized for finding habitable planets (0.5 to $10 M_{\text{Earth}}$) in the HZ (near 1 AU) of solar-like stars
- Continuously and simultaneously monitor **170,000** main-sequence stars
- Use a one-meter telescope: FOV $>100 \text{ deg}^2$ with an array of 42 CCD
- Photometric precision: Noise $< 20 \text{ ppm}$ in 6.5 hours $V = 12$ solar-like star
=> 4s detection for Earth-size transit
- Mission: Heliocentric orbit for continuous viewing ≥ 4 year duration



Milky Way Galaxy



Kepler Search Space

1 Kpc

Sun

Orion Spur

Perseus Arm

Sagittarius Arm

Goals of Kepler asteroseismology

- 170000 stars at low cadence (30 min)
- 512 stars at high cadence (1 min)
- Data for Radii Programme (KAI / KASOC)

2009 2010 2011 2012 2013 →

